

# AN ORDER LEVEL INVENTORY MODEL FOR A DETERIORATING ITEM WITH CONSTANT DETERIORATION, EXPONENTIAL DEMAND AND SHORTAGES

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# An Order Level Inventory Model for a **Deteriorating Item with Constant Deterioration**, **Exponential Demand and Shortages**

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Abstract – An Inventory model is developed for a deteriorating item with constant deteriorating rate having an instantaneous supply, an exponential demand and shortages in Inventory. The model is solved analytically to obtain the optimal solution of the problem. It is then illustrated with the help of numerical example. The sensitivity of the optimal solution towards changes in the values of different parameters is also studied.

#### INTRODUCTION 1. AND REVIEW OF LITERATURES

The aim of the paper is to develop an Economic order quantity Model (EOQ model) for a single item inventory having an exponential demand.

A brief review of the literature dealing with time varying demands is made in the following paragraphs.

In formulating inventory model, two factors of the problem have been growing interest to the researchers, one being the deterioration of the items and other being the variation in the demand rate with time. Silver and Meal(1969) developed an approximate solution procedure for the general case of the deterministic, time varying demand pattern. The classical no shortage inventory problem for a linear trend in demand over a finite time horizon was analytically solved by Donaldson (1977). However, Donaldson's solution procedure was computationally complicated. Silver (1979) derived a heuristic for a special case of a positive, linear trend in demand and applied it to the problem of Donaldson (1977). Ritchie (1980, 1984 and 1985) obtained an exact solution, having the simplicity of the EOQ formula, for Donaldson's problem for a linear increasing demand.

Mitra et al (1984) presented a simple procedure for adjusting the economic order quantity model for the case of increasing or decreasing linear trend in demand. possibilities of The shortage and deterioration in inventory were of left out consideration in all these models.

Dave and Paul (1981) developed an inventory model for deteriorating items with time proportional demand.

This model was extended by Sachan(1984) to cover the backlogging option. Bahari- Kaushari (1989) discussed a heuristic model for obtaining order quantities when demand is time proportional and inventory deteriorates at a constant rate over time. Deb and Chaudhuri (1987) studied the inventory replenishment policy for items having a deterministic demand pattern with linear (positive) trend and shortages; they developed a heuristic to determine the decision role for soliciting the items and sizes of replenishment over a finite time- horizon so as to keep the total costs minimum. This work was my Murdeshwar(1988), Subsequent extended contribution in this direction came from researchers. Like Goyal (1986, 1988), Dave (1989), Hariga (1994), Goswami and Chaudhari(1991), XU and Wang Chung and Ting(1993), Kim(1995), (1991), Hariga(1995, 1996), Jalan, Giri and Chaudhuri(1996), Jalan and Chaudhuri(1999), Lin, Ton and Lee (2000) etc.

These investigations were followed by several researchers like Shah and Jaiswal (1977), Aggarwal (1979), Roy – Chowhuri and Chaudhuri (1983). The Model Developed by Covert and Philip (1973), Philip (1974) and Mishra (1975) did not allowed shortages in inventory and used a constant demand rate.

Wee (1995) and Jalan and Chaudhuri (1999) worked with an exponentially time varying demand.

Recently Ghosh and Chaudhuri (2004) have obtained an inventory model for a deteriorating item with Weibull Distribution deterioration, time quadratic demand and shortages.

In the paper, we assume that time dependence of the demand rate is exponential. Deterioration rate is assumed to be a constant and shortages in the inventory are allowed. An analytical solution of the model is discussed and it is illustrated with the help of numerical example. Sensitivity of the optimal solution with respect to changes in different parameter values is also examined.

#### 2. NOTATIONS

The following notations are used in the model.

C<sub>1</sub>- inventory carrying cost per unit per unit time.

C2- Shortage cost per unit time

C<sub>3</sub>- ordering cost per order

C<sub>4</sub>- cost of a unit.

- I<sub>0</sub> Size of initial inventory
- K a constant value (0<K<1)
- $t_1$  time during which there is no shortage(0<t\_1<T)
- T\*- Optimal value of T
- $I_0^*$  Optimal value of  $I_0$
- $t_1^*$  optimal value of  $t_1$
- K\* Optimal value of K

#### **ASSUMPTIONS:** 3.

The following assumptions are used for this model;

- The Demand rate R(t) varies exponentially (i) with time . i.e R(t)= $\lambda_0 e^{\alpha t}$ ,  $\lambda_0 \alpha$  are constants
- (ii) Shortage in the inventory are allowed and completely backlogged.
- (iii) The supply is instantaneous and the lead time is zero.
- (iv) A deteriorateditem is not repaired or replaced during a given cycle.
- (v) The holding cost, ordering cost, shortage cost and unit cost remain constant over time.

#### 4. FORMULATION AND SOLUTION

The instantaneous State of the inventory level I(t) at any time t is governed by differential equations

$$\frac{\mathrm{dI}(t)}{\mathrm{dt}} + \theta.\,\mathrm{I}(t) = -\lambda_0 e^{\alpha t} \qquad 0 \le t \le t_1 \qquad (4.1)$$

With

and

$$\frac{dI(t)}{dt} = -\lambda_0 e^{\alpha t}, t_1 \le t \le T$$
(4.2)

 $I(0) = I_0$  and  $I(t_1) = 0$ 

with  $I(t_1) = 0$ 

The Solutions of Eq. (4.1)and Eq.(4.2 )are respectively given by

$$I(t) = \frac{\lambda_0}{(\alpha+\theta)} \left( e^{(\alpha+\theta)t_1 - \theta t} - e^{\alpha t} \right) 0 \le t \le t_1$$
(4.3)

and

$$I(t) = \frac{\lambda_0}{\alpha} (e^{\alpha t_1} - e^{\alpha t}) t_1 \le T$$
(4.4)

also

$$I_0 = \frac{\lambda_0}{(\alpha+\theta)} \left( e^{(\alpha+\theta)t_1} - 1 \right) = \frac{\lambda_0}{(\alpha+\theta)} \left( e^{(\alpha+\theta)KT} - 1 \right)$$

Since the length of the shortage interval is a part of the cycle time, we may assume

$$t_1 = KT, 0 < K < 1$$
 (4.5)

Where K is a constant to be determined in an optimal manner. Now we can write

$$I_0 = \frac{\lambda_0}{(\alpha + \theta)} \left( e^{(\alpha + \theta)KT} - 1 \right)$$
(4.6)

The Inventory level at the beginning of the cycle must be sufficient enough to meet the total demand aiven bv

$$\int_{0}^{t_{1}} \lambda_{0} e^{\alpha t} dt = \frac{\lambda_{0}}{\alpha} (e^{\alpha t_{1}} - 1)$$
(4.7)

The total quantity of deteriorated item is given by

$$I_0 - \frac{\lambda_0}{\alpha} (e^{\alpha t_1} - 1) \tag{4.8}$$

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## Average Inventory Holding Cost

The average inventory holding cost in  $(0, t_1)$  is

$$\frac{C_1}{T} \int_0^{t_1} I(t) dt = \frac{C_1}{T} \frac{\lambda_0}{(\alpha + \theta)} \int_0^{t_1} (e^{(\alpha + \theta)t_1 - \theta t} - e^{\alpha t}) dt$$

$$= \frac{c_1 \lambda_0}{\alpha \theta (\alpha + \theta) T} \Big( \Big( \theta + \alpha e^{(\alpha + \theta) t_1} \Big) - (\alpha + \theta) e^{\alpha t_1} \Big)$$
(4.9)

### Average Shortage Cost

The average shortage cost in  $[t_1, T]$  is given by

$$\frac{C_2}{T} \int_{t_1}^{T} \lambda_0 e^{\alpha t} (T-t) dt = \frac{\lambda_0 C_2}{\alpha T} \left[ \frac{1}{\alpha} (e^{\alpha T} - e^{\alpha t_1}) - (T-t_1) e^{\alpha t_1} \right]$$
(4.10)

### Average Ordering Cost

The average ordering cost is given by

$$\frac{C_3}{T}$$
 (4.11)

#### The Average Cost of Deterioration

Cost of deteriorating item per unit time is given by

$$\frac{C_4}{T} \left\{ I_0 - \frac{\lambda_0}{\alpha} \left( e^{\alpha t_1} - 1 \right) \right\} = \frac{\lambda_0 C_4}{T} \left\{ \frac{e^{(\alpha+\theta)t_1}}{(\alpha+\theta)} - \frac{1}{\alpha} e^{\alpha t_1} + \frac{\theta}{\alpha(\alpha+\theta)} \right\}$$
(4.12)

Average variable cost (AVC) per unit time is

AVC = 
$$\frac{\lambda_0 C_1}{\alpha \theta (\alpha + \theta) T} (\theta + \alpha e^{(\alpha + \theta)t_1} - (\alpha + \theta) e^{\alpha t_1})$$

$$+\frac{\lambda_0 C_2}{\alpha T} \left( \frac{1}{\alpha} (e^{\alpha T} - e^{\alpha t_1}) - (T - t_1) e^{\alpha t_1} \right) + \frac{C_3}{T} + \frac{\lambda_0 C_4}{T} \left( \frac{e^{(\alpha + \theta)t_1}}{(\alpha + \theta)} - \frac{1}{\alpha} e^{\alpha t_1} + \frac{\theta}{\alpha(\alpha + \theta)} \right)$$
(4.13)

Now

$$\begin{aligned} \mathbf{AVC} &= \frac{\lambda_0 C_1}{\alpha \theta (\alpha + \theta) \mathrm{T}} \left( \alpha \mathbf{e}^{(\alpha + \theta) \mathrm{KT}} - (\alpha + \theta) \mathbf{e}^{\alpha \mathrm{KT}} + \theta \right) \\ &+ \frac{\lambda_0 C_2}{\alpha \mathrm{T}} \left( \frac{1}{\alpha} \mathbf{e}^{\alpha \mathrm{T}} - (\mathrm{T} - \mathrm{KT} + \frac{1}{\alpha}) \mathbf{e}^{\alpha \mathrm{KT}} \right) + \frac{C_3}{\mathrm{T}} \\ &+ \frac{\lambda_0 C_4}{\mathrm{T}} \left( \frac{\mathbf{e}^{(\alpha + \theta) \mathrm{KT}}}{(\alpha + \theta)} - \frac{1}{\alpha} \mathbf{e}^{\alpha \mathrm{KT}} + \frac{\theta}{\alpha (\alpha + \theta)} \right) \\ &= \frac{\lambda_0}{\mathrm{T}} \left[ \frac{C_1 + C_4 \theta}{\theta (\alpha + \theta)} \mathbf{e}^{(\alpha + \theta) \mathrm{KT}} - \left\{ \frac{C_2 \mathrm{T} (1 - \mathrm{K})}{\alpha} + \frac{1}{\alpha} (\frac{C_1}{\theta} + \frac{C_2}{\alpha} + C_4) \right\} \mathbf{e}^{\alpha \mathrm{KT}} \right\} + \frac{C_2}{\alpha^2} \mathbf{e}^{\alpha \mathrm{T}} + \end{aligned}$$

$$\left(\frac{C_1 + C_4 \theta}{\alpha(\alpha + \theta)} + \frac{C_3}{\lambda_0}\right)$$
 (4.14)

Treating K and T as decision variables, the necessary conditions for the minimization of the average system cost are

$$\frac{\partial}{\partial T}(AVC) = 0 \qquad (4.15)$$

and

$$\frac{\partial}{\partial K}(AVC) = 0 \tag{4.16}$$

After a little calculation,  $\frac{\partial}{\partial T}$  (AVC) becomes

$$= \frac{\lambda_0}{T} \left( \frac{(C_1 + C_4 \theta)(\alpha + \theta)K}{\theta(\alpha + \theta)} e^{(\alpha + \theta)KT} + \frac{C_2}{\alpha} e^{\alpha T} - \left( \frac{C_1}{\theta} + \frac{C_2}{\alpha} + C_4 \right) K e^{\alpha KT} \right)$$
$$= \frac{\lambda_0}{T^2} \left\{ \frac{(C_1 + C_4 \theta)}{\theta(\alpha + \theta)} e^{(\alpha + \theta)KT} + \frac{C_2}{\alpha^2} e^{\alpha T} - \frac{1}{\alpha} \left( \frac{C_1}{\theta} + \frac{C_2}{\alpha} + C_4 \right) e^{\alpha KT} + \left( \frac{(C_1 + C_4 \theta)}{\alpha(\alpha + \theta)} + \frac{C_3}{\lambda_0} \right) \right\}$$
$$- \frac{\lambda_0 C_2}{\alpha} (1 - K) \alpha K e^{\alpha KT}$$

i.e

$$\frac{\partial}{\partial T} (AVC) = \frac{\lambda_0}{T^2} \left[ \frac{(C_1 + C_4 \theta)}{\theta} \left\{ KT - \frac{1}{(\alpha + \theta)} \right\} e^{(\alpha + \theta)KT} \right. \\ \left. + \left. \left\{ \frac{(\alpha C_1 + \theta C_2 + \alpha \theta C_4)(1 - \alpha KT) - C_2 \alpha^2 \theta (1 - K)KT^2}{\alpha^2 \theta} \right\} e^{\alpha KT} \right. \\ \left. + \frac{C_2 (\alpha T - 1)}{\alpha^2} e^{\alpha T} \right. \\ \left. - \left. \left( \frac{(C_1 + C_4 \theta)}{\alpha (\alpha + \theta)} \right) \right. \\ \left. + \frac{C_3}{\lambda_0} \right) \right]$$
(4.17)

Now (15) yields

$$\frac{(C_1+C_4\theta)}{\theta(\alpha+\theta)}\{(\alpha+\theta)KT-1\}e^{(\alpha+\theta)KT} - \left\{\frac{(\alpha C_1+\theta C_2+\alpha\theta C_4)(1-\alpha KT)}{\alpha^2\theta} - C_2(1-K)KT^2\right\}e^{\alpha KT} + \frac{C_2(\alpha T-1)}{\alpha^2}e^{\alpha T} - \left(\frac{(C_1+C_4\theta)}{\alpha(\alpha+\theta)} + \frac{C_3}{\lambda_0}\right) = 0$$
(4.18)

$$\frac{\partial}{\partial t}$$
 (AVC)

After a little calculation, 
$$\frac{1}{\partial K}$$
 (AVC) becomes

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$$\frac{\partial}{\partial K} (AVC) = \frac{\lambda_0}{T} \left[ \frac{(C_1 + C_4 \theta)}{\theta} T e^{(\alpha + \theta)KT} - \frac{T}{\alpha} e^{\alpha KT} \left\{ \alpha \left( \frac{C_1}{\theta} + \frac{C_2}{\alpha} + C_4 \right) + C_2 T (1 - K) \alpha - C_2 \right\} \right]$$

i.e

 $\frac{\partial}{\partial K}(AVC) = \frac{\lambda_0}{\theta T} \big[ (C_1 + C_4 \theta) T e^{\theta KT} - \{ (C_1 + C_4 \theta) + C_2 \theta T (1 - K) \} T \big] e^{\alpha KT}$ 

 $\frac{\partial}{\partial K}(AVC) = \frac{\lambda_0}{\theta}(C_1 + C_4\theta))e^{\theta KT} - \{(C_1 + C_4\theta) + C_2\theta(1 - K)T\}e^{\alpha KT} \quad (4.19)$ 

#### Now (16) yields

 $\alpha(C_1 + C_4\theta)e^{\theta KT} - C_2\alpha\theta(1 - K)T - \alpha(\theta C_4 + C_1) = 0$ (4.20)

#### We can easily calculate

$$\begin{split} \frac{\partial^{2}}{\partial T^{2}} (AVC) &= \frac{\lambda_{0}}{T^{3}} \Big[ \frac{(C_{1} + C_{4}\theta)}{\theta(\alpha + \theta)} \{ (\alpha + \theta)^{2} K^{2} T^{2} - 2(\alpha + \theta) KT + 2 \} e^{(\alpha + \theta) KT} \\ &- \frac{1}{\alpha} \Big\{ \Big( \frac{C_{1}}{\theta} + \frac{C_{2}}{\alpha} + C_{4} \Big) (\alpha^{2} K^{2} T - 2 \alpha KT + 2) + C_{2} \alpha^{2} (1 - K) K^{2} T^{3} \Big\} e^{\alpha KT} \\ &+ \frac{C_{2}}{\alpha^{2}} (\alpha^{2} T^{2} - 2 \alpha T + 2) + 2 \left( \frac{(C_{1} + C_{4}\theta)}{\alpha(\alpha + \theta)} + \frac{C_{3}}{\lambda_{0}} \right) \Big] \quad (4.21) \\ &\frac{\partial^{2}}{\partial K^{2}} (AVC) = \frac{\lambda_{0}}{\theta} \Big[ \alpha T \Big\{ (C_{1} + C_{4}\theta) e^{\theta KT} - \{ (C_{1} + C_{4}\theta) + C_{2}\theta(1 - K)T \} \Big\} e^{\alpha KT} \\ &+ \Big\{ \Big( C_{1} + C_{4}\theta \Big) \theta T e^{\theta KT} - \Big\{ -C_{2}\theta T \Big\} \Big\} e^{\alpha KT} \Big] \end{split}$$

$$= \frac{\lambda_0}{\theta} T \left[ (\alpha + \theta) (C_1 + C_4 \theta) e^{\theta KT} - \alpha \theta C_2 (1 - K) T + \theta C_2 - \alpha (C_1 + C_4 \theta) \right] e^{\alpha KT}$$
(4.22)

$$\frac{\partial^2}{\partial K \partial T} (AVC) = \frac{\lambda_0}{\theta} \left[ (\alpha + \theta) (C_1 + C_4 \theta) K e^{\theta KT} \right]$$

$$- \{ \alpha (C_1 + C_4 \theta) K + C_2 \theta (1 - K) (\alpha KT + 1) \} ] e^{\alpha KT}$$
(4.23)

The Optimal value of  $T^*$  of T and K<sup>\*</sup> of K are obtained by solving (4.18) and (4.20).

The sufficient conditions that these values minimize AVC (T,.K) are

$$\frac{\partial^{2}}{\partial T^{2}}(AVC) > 0; \qquad \frac{\partial^{2}}{\partial K^{2}}(AVC) > 0$$
(4.24)

and

$$\frac{\partial^2}{\partial T^2} (AVC) \cdot \frac{\partial^2}{\partial K^2} (AVC) - (\frac{\partial^2}{\partial K \partial T} (AVC))^2 > 0 \qquad (4.25)$$

Equations (4.18) and (4.20) can only be solved with the help of a computer oriented numerical technique for a given set of parameter values. Once  $T^*$  and  $K^*$ 

are obtained, we get  $t_1^*$  from (4.5). We may then use (4.6) to determine the optimal EOQ  $I_0^*$  and (4.14) to get the optimal average cost AVC<sup>\*</sup>.

#### 5. ILLUSTRATIVE EXAMPLES

#### Example1:

 $C_1=.001, C_2=5.0, C_3=10.0, C_4=4.0, \alpha=0.53, \lambda_{0=0.126}$ 

 $\theta$ =0.05 in appropriate units.

Equations (4.18) and (4.20) are now solved using above data. Based on these input data, the computer outputs are as follows:

K\*=.95909, T\*=2.4403, 
$$t_1$$
\*=2.3405,

 $I_0^* = .6909, \quad AVC^* = 58.3631$  (5.1)

Computer oriented technique provides

$$\frac{\partial^2}{\partial K^2} (AVC) = 5.5551 \qquad \frac{\partial^2}{\partial T^2} (AVC) = 1.4136$$

and

$$\frac{\partial^2}{\partial K \, \partial T} (AVC) = 0.0053 \tag{5.2}$$

at K=K\* and T=T\*

obviously (4.24) and (4.25) are satisfied. The value AVC\* is minimal.

#### Example2:

$$C_1=.001, C_2=6.0, C_3=15.0, C_4=4.0, \alpha=0.62, \lambda_0=0.132$$

 $\theta$ =0.07 in appropriate units.

Based on these input data, the computer outputs are as follows:

$$K^* = .95141, \quad T^* = 2.5650 \quad t_1^* = 2.4404 \tag{5.3}$$

 $I_0^* = .7395$  AVC\* = 91.9197 in appropriate units.

Corresponding to K= K\* and T=T\*, we have

$$\frac{\partial^2}{\partial K^2} (AVC) = 9.7363 \frac{\partial^2}{\partial T^2} (AVC) = 1.8665$$

and

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 $\frac{\sigma^2}{\partial K \partial T}$  (AVC) = 0.0153 (5.4)

The values are satisfied (4.24) and (4.25).

#### SENSITIVITY ANALYSIS 6.

We now study the effects of changes in the values of the system parameters  $C_1$ , C<sub>2</sub>,  $C_{3}$ C4, α.  $\lambda_0$  and  $\theta$  on the optimal cycle time, stock period, EOQ and Average variable cost derived by the proposed method. The sensitivity analysis is performed by changing each of the parameters by -50%, -20%, +20% and +50% taking one parameter at a time and keeping the remaining six parameters unchanged.

Table (Sensitivity Analysis)

	%				%	
Paramete	chang	% change	% change	% change in	change	%change
r	е	in t <sub>1</sub> *	in T*	I0*	in K*	in AVC*
C1	-50%	-0.0490	-0.0385	-0.0579	-0.0104	-0.0691
	-20%	-0.0197	-0.0156	-0.0289	-0.0042	-0.0269
	+20%	0.0206	0.0164	0.0289	0.0042	0.0269
	+50%	0.0483	0.0389	0.0724	0.0094	0.0708
	%	A/ 1			%	
Paramete	chang	% change	% change	% change in	change	%change
r	e	in t <sub>1</sub> *	in T*	I0*	in K*	in AVC*
C <sub>2</sub>	-50%	-29.3260	-34.8019	-38.5439	4.0622	13.9770
	-20%	-9.4385	-10.5893	-12.4041	1.0406	4.1177
	+20%	7.5749	8.2199	9.9580	-0.7027	-3.0533
	+50%	0.0000	0.0000	0.0000	0.0000	0.0000
	%				%	
Paramete	chang	% change	% change	% change in	change	%change
r	e	in t <sub>1</sub> *	in T*	I0*	in K*	in AVC*
C <sub>3</sub>	-50%	28.1902	28.2396	37.0531	-0.0688	57.6691
	-20%	9.5493	9.5710	12.5633	-0.0240	23.3744
	+20%	-8.1095	-8.1301	-10.6528	0.0191	-23.6571
	+50%	-18.3796	-18.4322	-24.1569	0.0444	-59.5268

	%				%	
	chang	% change	% change	% change in	change	%change
Parameter	e	in t <sub>1</sub> *	in T*	I0*	in K*	in AVC*
C4	-50%	-0.8294	1.2212	-1.0855	-2.0759	-17.7114
	-20%	-0.3331	0.4835	-0.4342	-0.8206	-7.0378
	+20%	0.3385	-0.4713	0.4487	0.8060	6.9763
	+50%	0.8517	-1.1630	1.1290	1.9915	17.3222
	%				%	
Paramete	chang	% change	% change	% change in	change	%change
r	e	in t <sub>1</sub> *	in T*	I0*	in K*	in AVC*
α	-50%	3.1186	3.1267	-21.9858	-0.0083	-0.5498
	-20%	-1.6718	-1.6760	-8.5975	0.0042	-0.8905
	+20%	2.9298	2.9369	6.6580	-0.0073	1.2165
	+50%	0.0000	0.0000	0.0000	0.0000	0.0000
	%				%	
Paramete	chang	% change	% change	% change in	change	%change
r	e	in t <sub>1</sub> *	in T*	Io*	in K*	in AVC*
λο	-50%	-32.1494	-32.2542	28.8754	0.0792	- 118.9263
	-20%	-9.9601	-9.9865	9.5383	0.0240	-29.1760
	+20%	7.8341	7.8523	-7.6422	-0.0198	19.0922
	+50%	17.0289	17.0635	-16.4134	-0.0417	37.7321
	%				%	
Paramete	chang	% change	% change	% change in	change	%change
r	e	in t <sub>1</sub> *	in T*	Io*	in K*	in AVC*
θ	-50%	-0.7677	1.3437	-2.1277	-2.1402	3.9318
	-20%	-0.3312	0.5245	-0.8540	-0.8602	1.5577
	+20%	0.3503	-0.5176	0.8684	0.8634	-1.5705
	+50%	0.9093	-1.2859	2.1277	2.1674	-3.9453

A careful study of above table1 reveals the following:

- K<sup>\*</sup>, T<sup>\*</sup>,  $t_1^*$ ,  $I_0^*$  and AVC<sup>\*</sup> increase (decrease) (i) with increase (decrease) in the value of parameters C<sub>1</sub> However K<sup>\*</sup>, T<sup>\*</sup>,  $t_1^*$ ,  $l_0^*$  and AVC\* are slightly sensitive to changes in C<sub>1</sub>.
- T<sup>\*</sup>,  $t_1$ <sup>\*</sup> and  $I_0$ <sup>\*</sup> increase (decrease) with the (ii) increase (decrease) in the value of parameters C2, whereas K\* and AVC\* increase (decrease) with decrease (increase) in the value of  $C_{2.}$  However  $T^{\ast},\,t_{1}^{\ast}\text{and }I_{0}^{\ast}$  are moderately sensitive and K\*, AVC\* are slightly sensitive to changes in C<sub>2</sub>.
- T\*,  $t_1^*$ ,  $I_0^*$  and AVC\* increase (decrease) with (iii) the decrease (increase) in the value of parameter C<sub>3</sub>. Whereas K\* increase (decrease) with the increase (decrease) in the value of  $C_3$ . However T<sup>\*</sup>,  $t_1^*$ ,  $I_0^*$  and AVC<sup>\*</sup> are moderately sensitive and K\* is slightly sensitive towards changes in C<sub>3.</sub>
- K\*,  $t_1^*$ ,  $I_0^*$  and AVC\* increase (decrease) with (iv) the decrease (increase) in the value of decrease parameter C<sub>4</sub> whereas T\* (increase) with the increase (decrease) in the value of C4. However AVC\* is moderately

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sensitive and K\*, T\*, t<sub>1</sub>\* and I<sub>0</sub>\* are slightly sensitive towards changes in C<sub>4</sub>.

- $K^*$  and  $I_0^*$  increase (decrease) with the (v) increase (decrease) in the value of parameter  $\alpha.$  whereas T\*,  $t_1^*$  and AVC\* decrease (increase) with the increase (decrease) in the value of  $\alpha$ . However  $I_0^*$  is moderately sensitive and K\*, T\*, t<sub>1</sub>\* and AVC\* are slightly sensitive towards the changes in  $\alpha$ .
- (vi) T\*, t1\* and AVC\* increase (decrease) with increase (decrease) in the value of parameter  $\lambda_0$  whereas K<sup>\*</sup> and I<sub>0</sub><sup>\*</sup> decrease (increase) with increase (decrease) in the value of  $\lambda_{0}$ . However T\*,  $t_1^*$ ,  $I_0^*$  and AVC\* are moderately sensitive and K\* is almost insensitive towards changes in  $\lambda_0$ .
- K\*, T\*,  $t_1^{\,*},\ I_0^{\,*}$  increase (decrease) with (vii) increase (decrease) in the value of parameter  $\theta$  whereas AVC\* increase (decrease) with the decrease (increase) in the value  $\theta$ . However K\*, T\*, t1\*, I0\* and AVC\* are slightly sensitive towards changes in  $\theta$ .

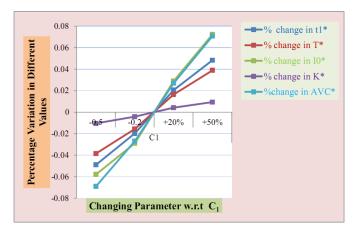


Fig 1 Percentage Variation in Parameter C<sub>1</sub>

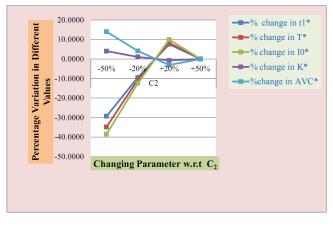
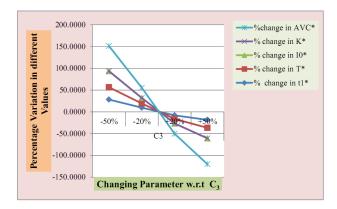
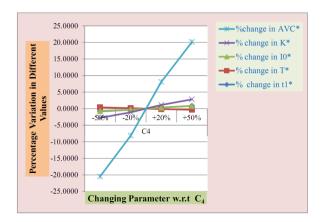


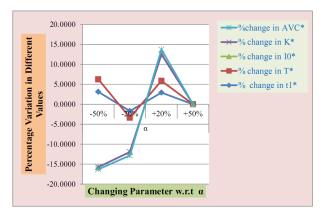
Fig 2 Percentage Variation in Parameter C<sub>2</sub>



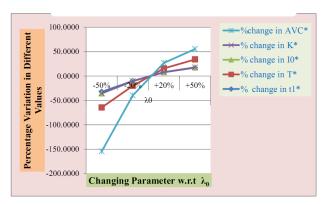
## Fig 3 Percentage Variation in Parameter C<sub>3</sub>





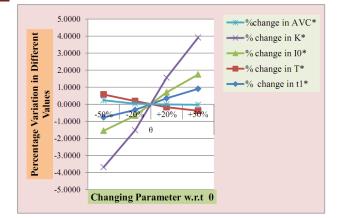






## Fig 6 Percentage Variation in Parameter $\lambda_0$

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### Fig 7 Percentage Variation in Parameter θ

## 7. CONCLUSION

The chapter is concerned with development of an inventory model for a deteriorating item with constant deteriorating rate having an instantaneous supply an exponential demand. Shortages are completely backlogged. The analytical approach is considered to obtain the optimal solution to minimise the average variable cost per time unit of the inventory system. It is illustrated with the help of numerical examples. Computer Oriented techniques is applied to solve the numerical problem. The effect of changes in the values of different parameters on the decision variable is studied.

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