

A Review of Mathematical Modeling Methods Currently Applied Within Healthcare Modelling and Implementation in Social Care

Mohammad Faisal Khan*

Assistant Professor, College of Science and Theoretical Studies, Saudi Electronic University, Riyadh, KSA

Abstract – *Mathematical modeling methods, with a concentration upon those methods presently applied inside healthcare modeling, and propose past and potential uses of these methods inside the field of social care. A rundown is offered of the model advancement process, including the utilization of issue organizing methods, writing checking on, elicitation and vulnerability investigation. Explicit modeling methods, for example, choice trees, state change models and discrete occasion reenactment are portrayed, with a diagram of their qualities and impediments. Current methodologies for measuring results inside wellbeing monetary assessment are additionally quickly talked about. The audit features specific issues maybe which ought to be viewed as while applying these modeling methods to social care.*

Keywords: *Mathematical Model, Social Care*

-----X-----

INTRODUCTION

In the health circle, mathematical modeling is a key device for basic leadership, especially when direct evaluation of intercessions isn't an alternative. Mathematical modeling is administered by a lot of conditions or rules depicting a genuine powerful framework and is reliant upon key suppositions about the connection between input parameters and results. While current mathematical modeling for general health purposes has gotten progressively unpredictable and refined after some time, we can follow its sources far back ever. During the 1700s, Swiss mathematician Daniel Bernoulli utilized smallpox mortality projections to present the defense for expanded immunization, even without a total comprehension of all affecting components.

Modeling is regularly the main reasonable and opportune alternative for illuminating fast basic leadership when direct experimentation is tedious, untrustworthy, or unrealistic, particularly while anticipating into what's to come. Randomized controlled preliminaries, considered the 'best quality level' for educating clinical choices, are not constantly plausible. Populace based reviews are helpful, yet they give just point gauges in the year in which information are gathered. Such studies, which can't extend into the future, regularly are not fueled to sub-national levels or disaggregated properly by age, constraining their utility. Conversely, modeling can represent changing socioeconomics after some

time, for example, maturing, just as fundamental elements, for example, mortality, and births.

Policy and health leaders are frequently urged to utilize a scope of devices and frameworks in supporting their staff while detailing and actualizing health arrangements. Interpretation of modeling information is key for successful correspondence between modelers, policy-producers and implementers. Albeit mathematical modeling has educated health policy choices in different health-related issues, look into use of genuine effect models could be low. In this way, reporting effective utilization of a far reaching structure for information interpretation of modeling to policy and writing computer programs is significant.

This survey displays an outline of mathematical modeling and its present and potential job in educating choices encompassing the administration and conveyance of social care. The reasons for the audit are triple:

1. To quickly depict the model advancement process and the most widely recognized methodological types of mathematical models used to illuminate health care policy basic leadership;
2. To survey the utilization of mathematical modeling in the evaluation of social care mediations, and;

3. To think about creating and applying existing modeling approaches inside a social care setting.

The utilization of mathematical models has increased a lot of unmistakable quality through their utilization in encouraging monetary evaluation (see join audit by Knapp 2011). In any case, models have likewise been utilized in various other basic leadership settings including hazard evaluation (Oscar 2004, Cook et al. 2006) and administration arranging and limit modeling (Vlachos et al. 2007, Andersson and Varbrand 2007). The methods talked about inside this survey are pertinent to any basic leadership setting; anyway the specific concentration here is upon healthcare monetary evaluation.

ROLE AND VALUE OF MATHEMATICAL MODELING

A mathematical model is a portrayal of this present reality, described by the utilization of arithmetic to speak to the pieces of this present reality that are of intrigue and the connections between those parts (Eddy 1985). Such models can be utilized to educate policy choices by orchestrating a different scope of proof inside a rational and express system. The utilization of mathematical models stays away from instinct alone and, now and again, the hazard, time and cost related with essential research. By definition, models include suspicion, reflection and rearrangements. Notwithstanding, presumptions can be had express and the effect of questionable suspicions upon the model outcomes can be officially evaluated. Mathematical models are created with the express capacity of advising basic leadership. Choice models create information on the normal expenses and results of elective approaches and the likelihood that a given choice option is ideal, given current information. Mathematical modeling rests inside a Bayesian system including the combination of all pertinent, frequently unique, information in the improvement, execution and understanding of the model and its outcomes (Spiegelhalter et al. 1999). Choice systematic models can by and large be described by three basic highlights: (1) the meaning of causal connections between marvels; (2) the utilization of some type of extrapolation, either the projection of transient information to longer-term results or the interpretation from halfway to ultimate results through characterized causal relationship, and (3) the amalgamation of proof from various sources.

While different applications exist, the two fundamental regions where mathematical modeling is utilized to educate policy choices in health and prosperity are monetary choice modeling and administration arranging modeling. Inside healthcare, the previous for the most part includes the calculated and mathematical portrayal of some fundamental illness characteristic history and the effect of a given

arrangement of intercessions upon that regular history to assess anticipated expenses and outcomes. The expenses and results are normally depicted as the steady cost per quality-balanced life year (QALY) increased over a lifetime skyline, despite the fact that illness explicit results may likewise be accounted for. The approaching SSCR audit on cost-viability investigation by Knapp (2011) gives additional information about the monetary structure where such models are utilized. The last use of modeling is less well-characterized, regularly including modeling frameworks crosswise over cross-sectional populace bunches inside some association based framework (for instance, a medical clinic ward) so as to recognize a few methods for development, for example, cost reserve funds, improved proficiency or shorter holding up times. The particular modeling methods depicted beneath are material to the two regions.

THE MODEL DEVELOPMENT PROCESS

In a conventional sense, the development of a mathematical model includes the accompanying five non-unmistakable gatherings of activities:

1. Understanding the decision issue;
2. Calculated modeling;
3. Model execution;
4. Model checking; and
5. Connecting with the decision

Significantly, model development isn't, nor should it be, a direct procedure; these five arrangements of activities may cover; for instance, model checking is fitting through the whole development process. This depiction of the model development process is to a great extent general sable over any modeling application.

MODEL IMPLEMENTATION

Model implementation includes the quantitative programming of a reasonable model inside some product stage. This stage may include significant cycle in accomplishing an exchange off between the apparent 'perfect' model and the 'best' model conceivable given the restrictions in the proof base. The most suitable modeling procedure is subject to the decision issue viable and the information necessities of the decision-creator; the most widely recognized modeling methods are portrayed on pages 5 to 9. Basic suppositions, for example, those around the extrapolation of preliminary results are required inside the quantitative model. While proof survey is suitable over the entire model development process, it is especially significant here regarding the distinguishing proof,

determination and utilization of relevant proof to advise the model parameters. In healthcare financial evaluation 'relevant proof' may incorporate data identifying with the adequacy of intercessions, costs, asset use, utility qualities, the study of disease transmission and an etiology, probabilities of occasions happening and longer term results (Glanville and Paisley 2010). Proof sources may incorporate randomized controlled preliminaries, observational data and routine data sources (for instance, medical clinic scene insights and unit cost sources). Preferably, a significant number of these parameters would be distinguished through precise, extensive and reproducible writing audits. Practically speaking be that as it may, time and asset imperatives frequently make such procedures doable just for key model parameters. Formal or casual methods of elicitation of clinical specialists might be required for explicit suppositions or model parameters where relevant writing is inaccessible (O'Hagan 2006).

MODELLING METHODS

In health financial evaluation and administration arranging, mathematical models may reflect the experience of people or companions of patients and might be assessed regarding occasions or discrete augmentations of time. An itemized scientific categorization of elective model structures is accessible from Brennan et al. (2006). By and by, the most well-known indications of mathematical models are decision-trees, state progress models and patient-level models. These three wide classes of models are delineated beneath.

Decision trees

Decision trees are perhaps the least difficult type of decision model. These are commonly associate models which implies that they pursue a partner of individuals over some stretch of time yet don't recognize singular attributes. This implies the probabilities of occasions happening inside the model are related with a 'normal' individual. Decision trees are comprised of a decision hub which depicts all conceivable decision choices, chance hubs which portray the likelihood of occasions happening subordinate upon the decision hub, and result hubs which portray the likelihood all things considered. Result hubs are determined utilizing a methodology known as 'collapsing back' by duplicating the opportunity hubs prompting that result (Drummond et al. 2005). Figure 1 shows a case of a decision tree, assessing the likelihood of getting pregnant in a gathering of explicitly dynamic 18-year olds who are either given, or not given, preventative counsel. Probabilities are illustrative as it were. In light of this decision tree, the likelihood of turning out to be pregnant offered no preventative guidance would in this manner be $0.016+0.006$ which likens to 2.2%, and the likelihood of turning out to be pregnant offered prophylactic guidance would be $0.008+0.008$

which compares to 1.6%. Expenses and results for each part of the tree would likewise be determined to appraise the distinction in expenses and contrast in results between the two alternatives, and henceforth the steady cost-viability proportion related with the two choices. Decision trees are valuable when a decision procedure can be effectively separated into a treelike structure, and occasions of intrigue happen once and over a brief timeframe. The upside of decision trees is that they are moderately easy to create and comprehend. In any case, decision trees are not suitable when an issue is increasingly intricate.

State transition models

Inside state progress models, occasions of intrigue are modeled as advances starting with one state then onto the next. The timeframe of the model is separated into cycles of time, for instance a year, and at each cycle there is a likelihood of staying in a similar state or advancing to an alternate state inside the model. The key supposition that will be that all individuals must exist inside one of a limited number of states at any one time. State progress models are generally accomplice models, in spite of the fact that they can likewise pursue singular patients.

For instance, interminable myeloid leukemia (CML) can be depicted by three clinical stages as the patient advances: incessant stage, quickened stage and ballistic stage. Inside a state change model of CML, all patients would exist inside one of these health states or in the dead state. Probabilities of changing between the states are allotted with the goal that patients can advance from incessant stage to quickened stage, from quickened stage to ballistic stage, and from ballistic stage to dead. Invert changes are unrealistic. There would likewise be a likelihood of biting the dust from different causes from any of the CML states. When an individual has arrived at the dead state, there would be a likelihood of 1 of staying in that state.

Discrete event simulation

Discrete event simulations (DES) are singular level models where events can be founded on the past encounters of the elements (for instance, individuals) inside the model and their attributes. Inside DES, timing is expressly modeled by computing when the following event will happen following the event of every event (Pidd 2004). Resources, for example, staff or medical clinic beds, can be unequivocally modeled utilizing shift designs.

The model starts at the General Practice medical procedure and pursues the patients' examples to the lab where they are inspected and evaluated. These evaluations are then sent to the 'call and

review' workplaces for preparing the outcomes and presenting them out on the ladies. Every element is allotted persistent attributes, for example, hidden infection statuses, which decide the resulting pathway of the elements. Each procedure (or 'work focus') inside the model is modified to expect time to be finished and staff to be accessible where fitting. The white boxes inside Figure 3 enable lines to create preceding each work focus if there are lacking resources accessible around then. Inside this model, the DES was grown with the end goal that the outcome pivot times firmly coordinated what occurred by and by. Alternatives for change were then tried inside the model as far as result pivot times (Pilgrim and Chilcott 2008).

Other modeling methods

There are a wide scope of other modeling methods which have not been applied as broadly inside healthcare. It isn't achievable to cover these methods here. Anyway two key methods will be quickly depicted: framework elements and specialist based modeling. Framework elements means to catch input circles inside frameworks by right off the bat mapping these connections diagrammatically, and besides utilizing differential conditions to speak to them mathematically. Inside healthcare, framework elements has primarily been applied to irresistible sickness modeling, where the intricate idea of an irresistible infection should be caught (Atun et al. 2007). Operator based modeling is another individual-level methodology which reproduces specialists, for instance patients, with conceivably versatile conduct as indicated by their condition. Inside the model, specialists can adjust their conduct as indicated by communications between one another and their condition. Operator based modeling has additionally been applied to irresistible ailments (Meng et al. 2010). It is imperative to take note of that while there are focal points and disservices of utilizing every one of the modeling methods laid out here, the decision of fitting modeling approach isn't in every case clear. For instance, there is an exchange off between the expanded adaptability related with singular level modeling, for example, DES and the expanded programming mastery, data and time prerequisites.

APPLICATIONS OF MATHEMATICAL MODELS IN SOCIAL CARE

A writing search was embraced to recognize past uses of mathematical models in social care. This audit was not proposed to be thorough. The point was to catch the sorts of mathematical models right now being created inside social care and the key issues related with social care modeling. Social Care Online was looked for financial evaluations utilizing the terms 'monetary evaluation', 'cost adequacy's or 'cost utility' inside the title. Moreover, the Health Technology Assessment (HTA) site was scanned for

any evaluations around social care utilizing the inquiry term 'social care'. Studies were incorporated on the off chance that they evaluated the cost adequacy of UK social care intercessions, which are not focused on youngsters and which are not given inside an essential care or a medical clinic based setting, utilizing a mathematical model. Inside this survey, the utilization of a 'mathematical model' is portrayed by: (1) the meaning of causal connections between marvels; (2) the utilization of some type of extrapolation, either the projection of momentary data to longer-term results or the interpretation from halfway to ultimate results through characterized causal relationship; and (3) the union of proof from different sources. 300 and seventy six conceivably relevant examinations were distinguished by the quests. Following title and theoretical filtering and in the wake of getting possibly relevant full papers, no investigations were recognized which utilized a mathematical model as characterized above to survey the cost-viability of social care intercessions. Five monetary evaluations close by clinical preliminaries were distinguished from the survey. The utilization of proof from just a single preliminary implies that all relevant comparators may not be incorporated inside the investigation. This is significant in light of the fact that it might be that the most financially alluring comparator is excluded inside the examination. Furthermore, it may not be conceivable to sufficiently catch the vulnerability around the populace mean. Also, extrapolation of preliminary results is critical to catch all distinctions in expenses and results between the mediation and the comparator. Utilizing just the preliminary data is probably going to think little of the distinctions in the two expenses and results, and thus will prompt various outcomes and possibly various ends. Extrapolation inside a mathematical model may include broadening results revealed inside the preliminaries over the long haul or it might include the estimation of ultimate results which have not been gathered inside the preliminary by modeling a connection among these and the middle of the road results gathered inside the preliminaries. For instance, assume a model of the effect of preventative guidance upon expenses and results is required, yet preliminary data are just accessible announcing prophylactic use. The model would need to catch the connection between prophylactic use and pregnancy rates, between pregnancy rates and birth rates, and the manner by which this effects upon health-related personal satisfaction.

CONCLUSION

This audit has portrayed the nonexclusive model development process and the most well-known use of mathematical models inside healthcare. A writing audit was attempted which proposes that, while some monetary evaluations are embraced close by clinical preliminaries inside social care, modeling which incorporates relevant proof and extrapolates

results past preliminary follow-up isn't commonly utilized inside social care. The modeling methods right now utilized inside healthcare could be applied to social care and there are clear advantages to doing this. In any case, further methodological development would be required as a component of the application to social care. Research around general health modeling might be valuable for applying modeling methods to social care since there are significant similitude's between the two applications

REFERENCES

- Andersson T. & Varbrand P. (2007). Decision support tools for ambulance dispatch and relocation, *Journal of the Operational Research Society*, 58, pp. 195–201.
- Atun R., Lebcirb R., McKeec M., Habichtd J., Cokerc R. (2007). Impact of joined-up HIV harm reduction and mulitdrug resistant tuberculosis control programmes in Estonia: system dynamics simulation model, *Health Policy*, 81, 2, pp. 207–217.
- Bojke L., Claxton K., Sculpher M., Palmer S. (2009). Characterizing structural uncertainty in decision-analytic models: a review and application of methods, *Value in Health*, 12, pp. 739–749.
- Brennan A., Chick S., Davies R. (2006). A taxonomy of model structures for economic evaluation, *Health Economics*, 15, 12, pp. 1295–1310.
- Briggs A., Sculpher M., Claxton K. (2006). *Decision Modelling for Health Economic Evaluation*, Oxford University Press Inc, New York.
- Charlesworth G., Shepstone L., Wilson E., Thalanany M., Mugford M., Poland F. (2008). Does befriending by trained lay workers improve psychological well-being and quality of life for carers of people with dementia, and at what cost? A randomised controlled trial, *Health Technology Assessment*, 12, p. 4.
- Chilcott J., Tappenden P., Rawdin A., Johnson M., Kaltenthaler E., Paisley S., Papaioannou D., Shippam A. (2010). Avoiding and identifying errors in health technology assessment models: qualitative study and methodological review, *Health Technology Assessment*, 14, 25, pp. 1–136.
- Claxton K., Posnett J. (1996). An economic approach to clinical trial design and research priority setting, *Health Economics*, 5, 6, pp. 513–524.
- Cook N., Buring J., Ridker P. (2006). The effect of including C-reactive protein in cardiovascular risk prediction models for women, *Annals of Internal Medicine*, 145, 1, pp. 21–29.
- Drummond M.F., Sculpher M.J., Torrance G.W., O'Brien B.J., Stoddart G.L. (2005). *Methods for the Economic Evaluation of Health Care Programmes*, Third edition, Oxford University Press, Oxford.
- Eddy D. (1985). Technology assessment: the role of mathematical modelling, in Mosteller F (ed.), *Assessing Medical Technologies*, National Academy Press, Washington, DC, pp. 144–160.
- Glanville J. & Paisley S. (2010). Chapter 7: Searching for evidence for cost-effectiveness decisions, in Shemilt I, Mugford M, Vale L, Marsh K, Donaldson C (eds.) *Evidence-based Decisions and Economics: Health care, Social Welfare, Education and Criminal Justice*, 2nd Edition, Wiley-Blackwell, pp. 79–92.
- Graff M., Adang E., Vernooij-Dassen M., Dekker J., Jönsson L., Thijssen M., Hoefnagels W., Olde Rikkert M. (2008). Community occupational therapy for older patients with dementia and their care givers: cost effectiveness study, *British Medical Journal*, 336, 7636, pp. 134–138.
- Kalra L., Evans A., Perez I., Knapp M., Swift C., Donaldson N. (2005). A randomised controlled comparison of alternative strategies in stroke care, *Health Technology Assessment*, 9, 18. Karnon J (2003) Alternative decision modelling techniques for the evaluation of health care technologies: Markov processes versus discrete event simulation, *Health Economics*, 12, pp. 837–848.
- Knapp M. (2011). Cost-effectiveness analysis and social care, *SSCR Methods Review* 16, NIHR School for Social Care Research, London.
- Mason A., Weatherly H., Spilsbury K., Arksey H., Golder S., Adamson J., Drummond M., Glendinning C. (2007). A systematic review of the effectiveness and cost-effectiveness of different models of community-based respite care for frail older people and their carers, *Health Technology Assessment*, 11, pp. 15.
- Meng Y., Davies R., Hardy K., Hawkey P. (2010). An application of agent-based simulation to the management of hospital-acquired infection, *Journal of Simulation*, 4, pp. 60–67.

- NICE (2008). Guide to the Methods of Technology Appraisal, National Institute for Health and Clinical Excellence, London.
- O'Hagan A. (2006). Research in elicitation, in Upadhyay SK, Singh U, Dey DK (eds) Bayesian Statistics and its Applications, Anamaya, New Delhi, pp. 375–382.
- Oscar T. (2004). A quantitative risk assessment model for Salmonella and whole chickens. *International Journal of Food Microbiology*, 93, 2: pp. 231–247.
- Patel A., Knapp M., Evans A., Perez I., Kalra L. (2004). Training care givers of stroke patients: economic evaluation, *British Medical Journal*, 328, pp. 1102–1104.
- Pidd M. (2004). *Computer Simulation in Management Science*, John Wiley and Sons Ltd, Chichester. Pidd M (2009) *Tools for Thinking; Modelling in Management Science*, John Wiley and Sons Ltd, Chichester.
- Pilgrim H. & Chilcott J. (2008). Assessment of a 7-day turn-around for the reporting of cervical smear results using discrete event simulation, *Journal of the Operational Research Society*, 59, 7, pp. 902–910.
- Robinson S. (2008). Conceptual modelling for simulation part I: definition and requirements, *Journal of the Operational Research Society*, 59, pp. 278–290.
- Sonnenberg F. & Beck J. (1993). Markov models in medical decision making, *Medical Decision Making*, 13, pp. 322–338.
- Speigelhalter D., Myles J., Jones D., Abrams K. (1999). An introduction to Bayesian methods in health technology assessment, *British Medical Journal*, 319, pp. 508–512.
- Vlachos D., Georgiadis P., Iakovou E. (2007). A system dynamics model for dynamic capacity planning of remanufacturing in closed-loop supply chains, *Computers & Operations Research*, 34, 2, pp. 367–394.
- Weatherly H., Drummond M., Claxton K., Cookson R., Ferguson B., Godfrey C., Rice N., Sculpher M., Sowden A. (2009). Methods for assessing the cost-effectiveness of public health interventions: key challenges and recommendations, *Health Policy*, 93, 2, pp. 85–92.

Corresponding Author

Mohammad Faisal Khan*

Assistant Professor, College of Science and Theoretical Studies, Saudi Electronic University, Riyadh, KSA