

# A Study of Mesh Density on the Surface of a Far Field Sphere

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**Abstract – A system for machine mesh generation is proposed for ocean modeling applications. The technique uses a typical methodology to engineer to explain the structure of the mapping domain. Using stereographic coordinates, the underlying sphere is parameterized. Coasts are then represented in stereographic parametric space with cubic splines. In the parametric plane with usable techniques, the mesh creation algorithm constructs the network. This approach allows coastlines to be imported from multiple databases and thus domains with highly variable duration scales to be created. The findings include meshes and computational models of different kinds.**

**Key Words: Mesh Generation, Sphere, Ocean Modeling**

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## INTRODUCTION

For several decades, finite elements were used for engineering research. Since the 1990s, computer-aided design (CAD) programmes have developed geometric domains that are employed in finite element analysis and design. The CAD structures today are exceptionally reliable: the bulk of the complicated geometric characteristics of electronic devices or assemblies are shielded. Standard ocean simulations are based on cartesian grids (Griffies et. al. 2000). It has recently been used in the simulation of oceans as discrete elements and unstructured meshes (e.g. Piggott et al. 2007, White et. al. 2008 and Danilov et. al. 2005). The freedom to interact with the shores is one of the benefits of unstructured grids. As unstructured grid ocean models emerged, mesh generation algorithms were built or adapted from traditional engineering methods. Le Provost et. al. (1994) use the Henry and Walters mesh generation software (1993) for the production of a world-wide mesh method for global mate modeling. Le Provost et. al. (1994). Moreover, Lyard et. al. (2006), with the state-of-the-art FES2004 tidal model, uses a higher-resolution variant of the same mesh kind. Two algorithms Hagen et. al. (2001) create coastal domain meshes and use them to form tides in the Mexican gulf. The high resolution meshes of the Great Barrier Reef (Australia) were provided by Legrand et. al. (2006). Legrand et. al. (2000) and Gorman et. al. (2007) also developed a global algorithm for meshes from the World Ocean.

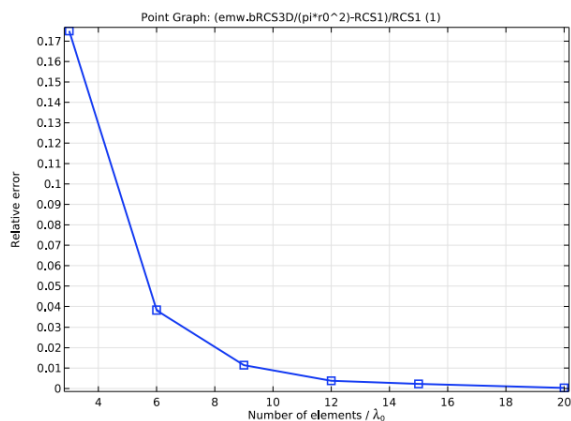
The Earth surface, i.e. an S sphere centered at the source within appropriate approximation and a Distance of approximately 6,370 km, is our area of

concern. There are nations and reefs on the coasts of the Global Seas. The first intention of this paper is to explain an automated process which can be used in a specified precision to construct a boundary representation (BRep), of the world ocean geometry. This technique utilizes numerous data sets: high-resolution shoreline databases (Wessel and Smith in 1996), national relief data (the 2006 NGDC), local map data, etc. While reliable data is possible, a BRep with the highest resolution possible cannot be built anywhere. In the latest global coastline database, for example, the resolution is about 50 m, resulting in a large number of tracking points (9,451,331). We may construct a model of adjustable geometrical precision. Many regions of the world's importance are debunked by the absolute geometrical precision possible, whereas others are approximated more poorly. Our approach also helps the information to be integrated with multiple data sets. Numerical computational approaches use mesh, i.e. debunked variations of the CAD paradigm domains. In this article, we agreed not to create a new algorithm for meshing, developed especially for marine finite elements. Here, we have agreed to construct a CAD model that can be used for any mesher surface. In the last decade, techniques for mesh generation progressed with the aim of communicating with CAD models directly. More precisely, some writers have created Gmsh: a three-dimensional finite-element mesh generator with combined pre- and after-processing equipment. Gmsh's unique existence has significantly expanded the meshing methods of its surface model for several thousand islands, plus hundreds of thousands of checkpoints. The paper

further discusses these unique functions. The paper is broken into three sections. The first segment addresses the process of constructing CAD ocean geometry models. The second portion outlines procedures for mesh production. We offer illustrative examples of different simulation data in the last section.

## MESH CONVERGENCE

A mesh convergence analysis is carried out in order to verify the wavelength corresponding to the first limit in the RCS plot in Figure 3 to ensure that the model converges in isotropic refinements to a single solution. In a parametric brush, the pattern is solved by the amount of mesh components per wavelength. In the PML, the mesh density is not modified radially (i.e. in the sweeping direction for the fabric) in the outer region. The PML is solved in this direction by 5 layers of elements which are enough to solve the radial path of the exponential damping. Consequently, when including further product levels, the PML error contribution cannot be reduced. It is because the PML doesn't completely absorb due to limited thickness and damping rather than mesh-density that the principal error contribution is made. The addition to the error in the measured RCS can therefore not be decreased as the mesh is polished. The mesh convergence as seen in Figure 4. The error seen is the gap between the RCS and the exact solution of the finite element model



The PML can generate an error contribution that cannot be removed by refinement of the mesh, as stated. As the convergence plot does not indicate inflation, this error contribution should be less than 0.1%.

## COMPUTING THE RADAR CROSS SECTION OF A PERFECTLY CONDUCTING SPHERE

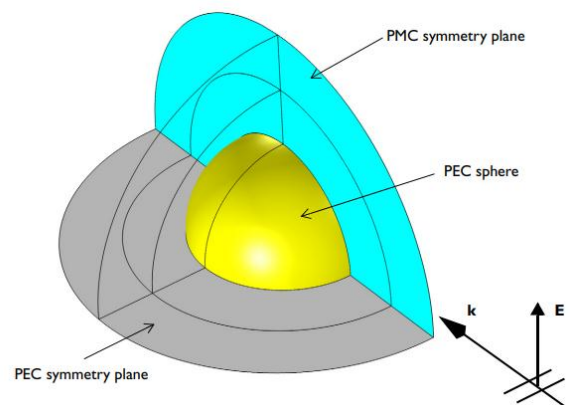
This is a typical issue in electromagnetic computation that requires the measurement, by a linearly Polarized Flatwave, of the monostatic radar cross section (RCS) of a perfectly conductive sphere in free space. The SCR is associated with an identical analytical solution and measured for the space radius-to-space wavelength ratios between 0.1 and 0.8. This region reflects the lower half of a boundary

field between the long asymptotic solution of wavelength, the "Rayleigh dispersion," and the short asymptotic solution for the asymptotic wavelength, the Geometrical Optics. For the first resonance of a scattering disc, a mesh convergence analysis is done with a ratio of about 0.16364 to free space wavelength.

## MODEL SETUP

### Geometry

Because of the symmetry, about a fifth of the sphere can be modelled. Geometry and border conditions are shown in Figure 1.



**Figure 1: The computational domain for computing the RCS of a PEC sphere in free space. Due to symmetry, it is sufficient to model one quarter of the sphere.**

Two concentric spherical shells compose of the structure. The innermost shell next to the sphere is the free space domain, and the second shell reflects an ideally balanced layer (PML) area used to provide the unbounded, in practice free space domain of roughly reflection-free termination.

## EQUATION

A Frequency Domain Formulation for the distributed electrical field is used to construct and overcome the concept. The incidence plane wave is travelling in the positive x direction and polarizing the electric field around the z axis. The frequency domain equation can be inserted in the format

$$\nabla \times (\mu_r^{-1} \nabla \times (\mathbf{E}_i + \mathbf{E}_{sc})) - k_0^2 \epsilon_{rc} (\mathbf{E}_i + \mathbf{E}_{sc}) = 0$$

Where Esc is the predictive variable and electric field is the dispersed electric field  $\mathbf{E}_i = (0, 0, E_z)$ , with

$$E_z = 1[V/m]e^{-jk_0x}$$

The equation is debunked by the usage of elements by second order edges (also classified as

vector elements, Nedelec elements or elements that correspond to curls). It is common knowledge that 10 or more choice points per wavelength should be tried in order to overcome the wavefield. This condition is met in some extent by integrating the usage of second-order elements and 8 elements per wavelength. A mesh is required on the scattering surface to make geometry marginally thinner for the longest wavelengths. At these boundaries a default unit size of half the radius is used. As mentioned in the section Perfectly matched sheet, special meshing is required in the PML region.

## BOUNDARY CONDITIONS

The field has ideal borders for the electric conductor (PEC). State of the PEC limit

$$\mathbf{n} \times \mathbf{E} = 0$$

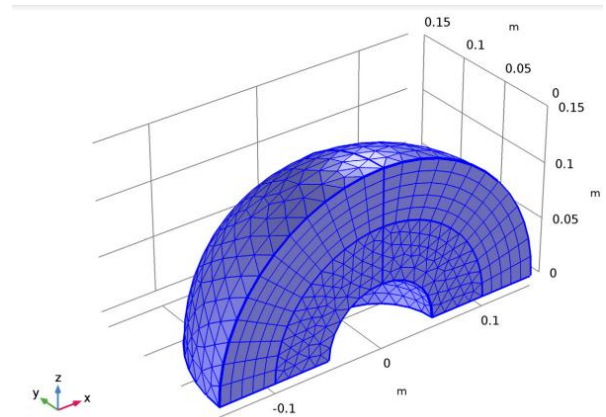
Sets the electric field's tangential part to zero. It is used for modeling metallic surfaces without loss or as the limiting condition of a symmetry form. Symmetry for electrical forces and electrical currents induced by them for magnetic fields and "magnetic waves" and counter symmetry. On symmetry planes used to subdivide model of sphere PEC limits and perfect Magnetic Conductor (PMC) limits.

$$\mathbf{n} \times \mathbf{H} = 0$$

Sets the magnetic field tangential component and hence the current surface density to zero. This can be viewed on exterior borders as a "high surface impedance" state or as a border state of symmetry. It imposes symmetry on electric fields, electric currents and ant symmetry on magnetic fields."

## PERFECTLY MATCHED LAYER

Approximately reflectively free termination of the programme domain is feasible in the area PML, the 2nd condensed shell across the sphere, by utilizing a dynamic coordinative extension in a radial direction. At least five elements by the thickness of the PML should be present for reasonable accuracy. Using a swept mesh to do this more easily, such that the efficient aspect output becomes resistant to radial scaling. Figure 2 shows the mesh used in this illustration. This is a free tetrahedral mesh and a swept mesh around the sphere of PML.



**Figure 2: A free tetrahedral mesh is used in the free-space region around the sphere, and a swept mesh is used in the PML region.**

It is known as the far-field area around the sphere. This states that a near-field approximation is carried out on the edge of this area that takes the electrical field measured across the sphere and uses the Stratton-Chu method to determine the dispersed electric field well away from its source.

In 3D, this is:

$$\mathbf{E}_p = \frac{jk}{4\pi} \mathbf{r}_0 \times \int [\mathbf{n} \times \mathbf{E} - \eta \mathbf{r}_0 \times (\mathbf{n} \times \mathbf{H})] \exp(jk \mathbf{r} \cdot \mathbf{r}_0) dS$$

In the case of dispersing difficulties, the far-flung region of COMSOL is close to what is recognized of physics as the "scattering amplitude.", while the far-field point p is taken at infinity also with an angular location well established  $(\theta, \phi)$ .

## A geometric model for the World Ocean

Every 3D model can be described by its BRep: the volume is restricted (called region) by the collection of surfaces and the area is restricted by a series of curves; two end points are contained in the curve. Three forms of concept entities are also used: vertices of the concept  $G_i^0$  (dimension 0), model edges  $G_i^1$  (dimension 1), and model surfaces  $G_i^2$  (dimension 2). Component entities are topological, i.e., only neighboring entities in the process are shielded. Each model entity must be linked with a geometry. They are formed by the geometries of curves and surfaces. Forms are commonly usable for parameterization, usually a projection. The parameterization determines the geometry of a sample edge as its underlies:

$$t \in \mathcal{R} \mapsto p(t) \in \mathcal{R}^3.$$

Similarly, the surface of the model is geometrically dependent on the parameterization specified surface:

$$(u, v) \in \mathcal{R}^2 \mapsto p(u, v) \in \mathcal{R}^3.$$

If a region has a slope, it is normally drawn on the surface area  $(u, v)$  parameter:

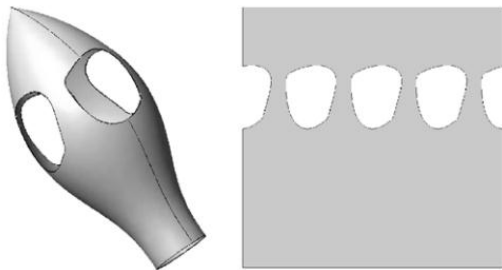
$$t \in \mathcal{R} \mapsto (u(t), v(t)) \in \mathcal{R}^2 \mapsto p(u(t), v(t)) \in \mathcal{R}^3.$$

Let's use the surface displayed in Fig as an example.

3. The following description illustrates the most critical features of concept entities:

- Intermittent surface layer. In the list of boundaries of the floor, a seam curve was added to better describe its closure.
- The surface is cut: there are four holes and the edge is cross-crossed by one of those holes.
- One of the edges of the image is degenerated when covering the sample profile. To take account of geographical peculiarities, degenerated boundaries have been used. In certain surface geometries, such degeneration occurs: triangles, cones, and even other groundbreaking surfaces.

The geometry of the ocean has been sliced from an engineering point of view



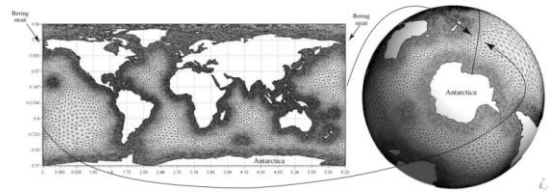
**Fig. 3 A model surface in real (left) and parametric (right) coordinates. The seam of the surface is highlighted in the left plot**

Sphere i.e. a periodic matrix surrounded by continents and reefs, with degeneration on the two poles.

## PARAMETRIZATION OF THE SPHERE

For the sphere, there are some conditions. Sphere coordinates are used for CAD schemes. Most of the data accessible in geosciences may be represented by means of a spatial method of the same features as the spherical coordinate system. Sphere coordinates experience many of the problems described earlier: there are two specific mapping points due to the existence of two degenerated models edges; one co-ordinate is intermittent,

contributing to one seam edge being introduced; the coastlines are capable of crossing the seam side, contributing to difficulty in determining geometry. The fabric edge cannot be preferred such that no shoreline is reached. In the photo. 4, the Planet Ocean mesh created with the spherical coordinate system is shown. The seam travels across the Strait of Bering across the Pacific and finishes somewhere on the Antarctic coastline. In comparison, like other dimensions, the spherical co-ordinates are not conformal. The angle at which curves cross one another is preserved by conformal mapping. Consequently, an isotropic mesh must be built on the parametric plane in order to have an isotropic mesh in real space. The visualization is extremely skewed at the singularities, i.e. near the poles in the case of spherical coordinates.



**Fig. 4 Mesh of the World Ocean using the spherical coordinate system. The seam edge is visible on the right plot**

## CONCLUSION

We found that the Wiscombe criteria explicitly underestimates the number of multiples required for nearby-field and some distant properties. In the case of most electromagnetic properties of concern on the far and close side, our proposed collection of three parameters resolve this issue. It is important to verify with these metrics how precise they are in determining the properties. The accuracy reached (by using a double precision calculation) is constrained by the amount of errors in the arithmetic for floating points and not by the early end of the sequence.

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