

Study of Complete and Incomplete Fusion of Weakly Bound Nuclei at Near Active Galactic Nuclei

Sarita Rani^{1*} Dr. Vipin Kumar²

¹ Research Scholar of OPJS University, Churu, Rajasthan

² Professor, OPJS University, Churu, Rajasthan

Abstract – We propose another quantum mechanical strategy to assess total and inadequate fusion in crashes of weakly bound nuclei. The strategy is applied to the $7\text{Li} + 209\text{Bi}$ system and the results are contrasted with trial data. The general understanding among hypothesis and test is awesome, above and underneath the Coulomb barrier. We discuss our present comprehension of the impact of the separation of stable weakly bound nuclei on the fusion cross section of these projectiles with light, medium and substantial mass targets, at energies over the Coulomb barrier. The discussion depends generally on data acquired by our gathering in cooperative examinations. We show that for overwhelming targets there is finished fusion concealment, relating to the event of inadequate fusion of one of the separation fragments, while for medium and light mass targets, there is no such impact, because of the insignificant deficient fusion process.

The classical dynamical model for reactions incited by weakly-bound nuclei at close barrier energies is grown further. It permits a quantitative investigation of the job and significance of fragmented fusion elements in asymptotic observables, for example, the number of inhabitants in high-turn states in reaction items just as the precise appropriation of direct alpha-creation. Model figurings show that fragmented fusion is a successful component for populating high-turn states, and its commitment to the direct alpha creation yield reduces with diminishing energy towards the Coulomb barrier.

Keywords: Complete and Incomplete Fusion, Weakly Bound Nuclei, Active Galactic Nuclei

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INTRODUCTION

The accessibility of radioactive pillars opened new conceivable outcomes in atomic material science. Specifically, crashes of pitifully bound cores have excited extraordinary intrigue, both hypothetical and trial, over the previous decade [1]. In such impacts, the breakup cross segment will in general be extremely huge and breakup couplings may affect the cross segments for a few different channels. A significant model is the fusion procedure, which for this situation turns out to be substantially more mind boggling, as, notwithstanding the standard fusion response, where the entire shot converges with the target to shape the compound core, there are other fusion forms following the breakup of the feebly bound crash accomplice. There is the likelihood that at least one, however not all, fragments are consumed by the target, while part of the shot's mass escapes the connection locale. It can likewise happen that all the shot's fragments are consecutively consumed by the target, delivering a similar compound core as on account of direct fusion. These fusion forms get various names. At the point

when the compound core doesn't contain the entirety of the shot's nucleons, we utilize the term fragmented fusion (ICF), while the fusion of the entirety of the shot's nucleons with the target is called finished fusion (CF). The CF cross segment is the whole of the cross area for the immediate fusion of the shot with the target (DCF) and of the successive fusion of the entirety of the shot's fragments (SCF). Most tests measure just the all out fusion (TF) cross area, which is the aggregate of the cross segments for CF and ICF. In any case, for some specific shot target mixes, it is conceivable to perform separate estimations of the cross areas for CF and ICF. Significant models are the fusion responses $6,7\text{Li} + 209\text{Bi}$ [2,3] and $9\text{Be} + 208\text{Pb}$, where the impact of the breakup channel on fusion was demonstrated to be solid. Numerous hypothetical methodologies have been proposed to consider fusion responses with feebly bound cores, going from basic traditional models to full quantum-mechanical figurings, utilizing the continuum undermined coupled channel strategy (CDCC). In most CDCC figurings fusion is incorporated by

methods for short range fanciful possibilities following up on each fragment. Along these lines, there is no connection between's ingestions of various fragments. In this way, one can't know whether the assimilation by one of these possibilities adds to ICF or to CF. Therefore, the computation gives just the added cross area for these procedures, σ_{TF} . This deficiency is maintained a strategic distance from in the CDCC figurings of Hagino et al. [7] and Diaz-Torres and Thompson [8]. These works embrace a solitary nonexistent potential following up on the full shot and trait ingestion in the bound channels to CF and assimilation in directs in the continuum to ICF. In any case, this technique may possibly be here and there defended when the consumed fragment contains an enormous part of the shot's mass. For this situation, the focal point of mass of the shot is near the focal point of mass of the substantial fragment, and it might be a decent estimation to expect that the overwhelming fragment is assimilated at whatever point the shot is inside the scope of the fanciful potential. This is the situation of ^{11}Be , which was the shot in the computations. For this situation, the breakup response is $^{11}\text{Be} \rightarrow n + ^{10}\text{Be}$ and ICF relate to the fusion of the ^{10}Be fragment with the target. Be that as it may, this strategy can't be utilized when the shot separates into fragments of practically identical masses. In such cases, a shot target nonexistent potential for unbound channels is good for nothing. The focal point of mass of the shot of the separated shot might be inside the scope of the fanciful potential with the two fragments being far away. Along these lines, there are no quantum-mechanical techniques to assess CF and ICF cross segments for impacts of feebly bound shots that separate into fragments of practically identical masses, as ^6Li or ^9Be , and the improvement of new strategies to assess CF and ICF cross segments that fuse quantum impacts is called for.

RESEARCH METHODOLOGY

Classical Dynamical Model

The classical dynamical model used to depict nuclear reactions involving loosely bound nuclei depends on the supposition that the projectile–target relative movement can be dealt with classically. Inside this methodology, when a weakly bound projectile is occurrence on target T with energy E_0 and orbital precise force L_0 , its movement is along a determinate way with distinct separation of nearest approach $R_{\min}(E_0, L_0)$. The way of the projectile is followed by settling the classical condition of movement affected by shared Coulomb and nuclear powers between the projectile and target. This interaction creates a Coulomb barrier for head-on ($L_0=0$) impacts of tallness at a V_B^{PT} partition R_B^{PT} . Since projectile is weakly bound it is exceptionally inclined to separate and the procedure of breakup of projectile is thought to be totally irregular procedure.

Let $P_{BU}^L(R)$ be the thickness of nearby breakup likelihood with the end goal that the likelihood of breakup of

projectile in the district R to $R+dR$ is $P_{BU}^L(R)dR$, R being the projectile target relative partition. For such a breakup occasion to happen there must be a limited likelihood of enduring the projectile in the interim ∞ to R, let it be $S(R)$. Presently it is very evident that $S(R+dR) = S(R)[1 - P_{BU}^L(R)dR]$ speaks to the likelihood of endurance of projectile at $R+dR$.

Modifying terms, we have

$$\frac{S(R+dR) - S(R)}{dR} = -S(R)P_{BU}^L(R)$$

$$\frac{dS(R)}{dR} = -S(R)P_{BU}^L(R)$$

At $R=\infty$, the projectile must endure that is $S(\infty)=1$. Under this boundary condition the above condition i.e.

$$\frac{dS(R)}{S(R)} = -P_{BU}^L(R)dR$$

Can be handily coordinated to give

$$S(R) = \exp\left[-\int_{\infty}^R P_{BU}^L(R)dR\right]$$

If $\int_{\infty}^R P_{BU}^L(R)dR \ll 1$ at that point $S(R)$ might be approximated, by holding just initial two terms of exponential extension, as

$$S(R) \approx 1 - \int_{\infty}^R P_{BU}^L(R)dR$$

What's more, the breakup likelihood at R which is essentially $1-S(R)$, is given by

$$P_{BU}(R) \approx \int_{\infty}^R P_{BU}^L(R)dR.$$

Since the breakup may happen either when the projectile is drawing nearer to the target or when it is leaving from the target in the wake of crossing, we may compose

$$P_{BU}(R_{\min}) = 2 \int_{R_{\min}}^{\infty} P_{BU}^L(R)dR.$$

On the observational ground or based on the CDCC counts, it is discovered that the vital in above condition can be communicated as an exponential capacity of separation of nearest approach that is

$$P_{BU}(R_{min}) = A \exp(-\alpha R_{min})$$

It promptly prompts the way that the neighborhood breakup work at any self-assertive R has a similar exponential structure

$$P_{BU}(R) \propto \exp(-\alpha R)$$

The situation of breakup of the projectile on its circle is dictated by inspecting a breakup range R_{BU} on the interim $[R_{min}(E_0, L_0), \infty]$ with the weighting $P_{BU}(R)$ which obviously place most R_{BU} in the region of R_{min} . It is significant that if the picked L_0 is not exactly the basic halfway wave for projectile fusion, L_{cr} , at that point the related direction would regularly prompt CF, i.e., $R_{min} \leq R_B^{PT}$. For these L_0 , R_{min} is set to be R_B^{PT} , when sampling R_{BU} , and all breakup occasions are limited to the approaching part of the projectile direction. Then

again for $L_0 > L_{cr}$ breakup can occur on both the passage and the leave parts of the classical circle, which are sampled similarly. Along these lines the function given by Eq. is utilized as an examining function to decide the position on the direction at which the projectile gets separated quickly into constituent fragments F1 and F2. For effortlessness, it is accepted that the interaction of fragments with the target and with one another can be depicted by a two-body focal potential. At the breakup position the dynamical factors like between fragment partition, relative precise force of fragments and the all out inside energy of the energized projectile are totally decided through Monte Carlo reenactment. At first the partition between two fragments in the projectile is determined by utilizing outspread likelihood conveyance which thus is gotten by utilizing a Gaussian function for the spiral piece of ground state wave function of the projectile. This Gaussian guess is all around advocated for 0+ ground condition of the projectile. The direction of between fragment partition is isotropic that is it might be picked arbitrarily over 4π strong point. The relative precise energy of fragments is sampled consistently on the

interim $[0, \ell_{max}]$; what's more, its direction is picked arbitrarily among the directions symmetrical to the direction of interfragment division. As to inner energy, based on quicker intermingling and comparable results rather than a uniform function, an exponentially diminishing function is picked to test it between the highest point of the barrier and a picked most extreme

ℓ_{max} . It merits referencing that both ℓ_{max} and ϵ_{max} are expanded until the intermingling happens. Presently the immediate max $\square$ speed of the fragments and the target in the focal point of mass edge at the purpose of breakup is controlled by utilizing energy, straight force and rakish energy preservation laws. After the breakup, the two body framework turns into a three body framework and the partition between the three bodies just as that among projectile and target is known. The all out energy of the three body framework is given by $E_{tot} = \epsilon_{12} + U_{1T}(r_{1T}) + U_{2T}(r_{2T}) + P_{PT}^2 / 2\mu_{PT}$ is rationed and is equivalent to the all out energy $E_{tot} = \frac{m_P}{m_T + m_P} E_0$ in the general center of-mass (CM) framework. Here ϵ_{12} is the overall energy of the fragments of the projectile, U_{12T} is interaction potential between fragment 1(2) and P_{PT} the target and is the relative direct force of the projectile and target. The energy protection promptly gives the modulus of relative speed among P and $T (V_{PT} = P_{PT} / \mu_{PT})$.

The information on $\tilde{v}_P$ and $\tilde{v}_T$, speeds of P and T as for in general CM, is required for giving starting condition to resulting engendering of three bodies in time. These speeds are identified with one another through

$$\tilde{v}_T = -\frac{m_P}{m_T} \tilde{v}_P$$

$$\vec{V}_{PT} = \tilde{v}_P - \tilde{v}_T$$

The extent of speed $\vec{V}_{PT}$ is now known through energy preservation, its direction is dictated by utilizing protection of precise force. The absolute rakish energy $\vec{L}_{tot} = \vec{\ell}_{12} + \vec{L}_{PT}$ in by and large CM framework is known as $\vec{L}_{total} = m_P b_0 (\vec{v} - \vec{V}_{CM})$ Here $\vec{\ell}_{12}, b_0, \vec{v}$ and $\vec{V}_{CM}$ are the relative rakish energy of the fragments of projectile, sway parameter, speed of projectile in research center framework and the CM speed individually. The $\vec{L}_{PT}$, rakish energy related with relative movement of P and T about CM, is referred to and is composed as

$$\vec{L}_{PT} = m_P \vec{R}_{PT} \times \tilde{v}_P$$

Presently parting $\tilde{\vec{v}}_p$ in spiral and transverse segment, we may compose

$$\tilde{\vec{v}}_p = \tilde{\vec{v}}_p^{(r)} \vec{r} + \tilde{\vec{v}}_p^{(q)} \vec{q}$$

With $\vec{r} = \vec{R}_{PT} / R_{PT}$ and $\vec{q} = \vec{n} \times \vec{r}$ when $\vec{n} = \vec{L}_{PT} / L_{PT}$. The transverse part of the speed of projectile and target are given by

$$\tilde{\vec{v}}_p^{(q)} = L_{PT} / (m_p R_{PT})$$

And

$$\tilde{\vec{v}}_T^{(q)} = -L_{PT} / (m_T R_{PT})$$

Separately. Presently utilizing Eq, it is very straight forward to acquire the accompanying articulation for outspread speed part

$$\tilde{\vec{v}}_p^{(r)} = \pm \frac{\left\{ V_{PT}^2 - \left[\tilde{\vec{v}}_p^{(q)} \left(1 + \frac{m_p}{m_T} \right) \right]^2 \right\}^{1/2}}{\left(1 + \frac{m_p}{m_T} \right)}$$

These speed and position vectors of the fragments of the projectile and target are changed to the research facility framework utilizing Galilean transformation. The essential system to numerate the ICF, CF and NCBU occasions is to expect that a fragment is melded with the target if the direction takes it inside the fragment target barrier range. Leave N alone the quantity of breakup occasions sampled and N_0 , N_1 and N_2 be the quantity of occasions with 0, 1 and 2 caught fragments individually, at that point the proportion $\tilde{P}_i = N_i / N$ [$i=0$ (NCBU), 1(ICF) or 2(CF)] gives the general yields of these three procedures with $\tilde{P}_0 + \tilde{P}_1 + \tilde{P}_2 = 1$ what's more, the supreme probabilities for these procedures are

$$P_0(E_0, L_0) = P_{BU}(R_{min}) \tilde{P}_0$$

$$P_1(E_0, L_0) = P_{BU}(R_{min}) \tilde{P}_1$$

$$P_2(E_0, L_0) = [1 - P_{BU}(R_{min})] H(L_{cr} - L_0) + P_{BU}(R_{min}) \tilde{P}_2$$

With $H(x)$ as the Heaviside step function and L_{cr} as the basic incomplete wave for fusion. The primary term

in the declaration of $P_2(E_0, L_0)$ relates to finish fusion (DCF) while the second one to successive complete fusion (SCF). The cross sections for these procedures are determined by utilizing keeping standard remedy

$$\sigma_i(E_0) = \pi \lambda^2 \sum_{L_0} (2L_0 + 1) P_i(E_0, L_0)$$

Where $\lambda^2 = \hbar^2 / (2\mu E_0)$ is the de-Broglie wavelength and $\mu = m_p m_T / (m_p + m_T)$ is the decreased mass of the projectile-target framework. This model is executed in the code PLATYPUS. In spite of the fact that this strategy is very fruitful in clarifying the CF, ICF and TF information at above barrier energies yet comes up short at around and sub barrier energies. The disappointment of the model at around and sub barrier energies might be ascribed to the way that at these energies the quantum mechanical tunneling impact gets critical and can't be overlooked. Here we have fused quantum mechanical tunneling revision dependent on WKB estimation right now.

WKB APPROXIMATION AND TUNNELING FACTOR

The WKB strategy depends on the development of wave function in forces of $\hbar$ what's more, is very valuable for rough arrangement of quantum mechanical issues in proper cases. Consider the accompanying fundamental Schrödinger wave equations in a single measurement

$$\frac{d^2 u}{dx^2} + k^2(x) u = 0 \quad \text{for } k^2 > 0$$

$$\frac{d^2 u}{dx^2} - \gamma^2(x) u = 0 \quad \text{for } \gamma^2 > 0$$

Such that

$$k(x) = \frac{1}{\hbar} \sqrt{2\mu(E - V(x))} \quad \text{when } V(x) < E$$

And

$$\gamma(x) = \frac{1}{\hbar} \sqrt{2\mu(V(x) - E)} \quad \text{when } V(x) > E$$

Are in every case genuine. For accommodation, let us accept that

$$u(x) = A \exp\left(\frac{i}{\hbar} S(x)\right)$$

Be the arrangement of Eq. which on substitution results is

$$\left(\frac{dS}{dx}\right)^2 - i\hbar \frac{d^2 S}{dx^2} - k^2 \hbar^2 = 0$$

Presently growing $S(x)$ in forces of $\hbar$

$$S(x) = S_0(x) + S_1(x)\hbar + S_2(x)\frac{\hbar^2}{2} + \dots$$

Subbing the extension in Eq. what's more, comparing the coefficients of terms having $\hbar$ raised to control one, we get

$$-S_0'^2 + 2\mu(E - V) = 0$$

And

$$iS_0'' - 2S_0'S_1' = 0$$

This Eq. might be revamped as

$$S_0'^2 - k^2 \hbar^2 = 0$$

And

$$S_1' = \frac{ik'}{2k}$$

Mix of Eq. quickly gives

$$S_0(x) = \pm \hbar \int^x k(x') dx'$$

What's more, that of Eq. gives

$$S_1 = \frac{i}{2} \ln k(x)$$

Here the self-assertive constants of joining are excluded on the grounds that these might be caught up in A. Presently on the off chance that lone initial two terms in the extension of S are held, at that point

$$u = A \exp\left(\frac{i}{\hbar} S_0\right) \exp(iS_1)$$

Utilizing Eq. we get

$$u(x) = \frac{A}{k^{1/2}} \exp(\pm i \int^x k dx) \quad \text{for } V < E$$

Essentially the estimated arrangement of Eq. is

$$u(x) = \frac{B}{\gamma^{1/2}} \exp(\pm \int^x \gamma dx) \quad \text{for } V > E$$

These arrangements might be dealt with exact in

that piece of the area of x where $\left|\frac{k'}{2k^2}\right| \ll 1$ that is the point at which the potential energy changes so gradually that the force of molecule is constantly consistent over numerous wavelengths. Yet, this condition doesn't hold great close to defining moment and henceforth these inexact arrangements are asymptotically substantial. Since wave Eq. are customary at a defining moment there are systematic arrangements at these focuses which have above asymptotic structure. So as to discover accurate arrangement having wanted asymptotic structure consider that the source of x lies at a defining moment, to one side of the defining moment (positive $V(x) \neq E$) and that

$$\xi(x) \equiv \int_0^x k dx$$

Now if $k^2(x) = Cx^n$, C being certain steady, Eq. have arrangements

$$u(x) = A \sqrt{\frac{\xi}{k}} J_{\pm m}(\xi), \quad m = \frac{1}{n+2}$$

With as a Bessel function and it concurs asymptotically with Eq.. To J confirm this let us modify Eq. with an extra term $\theta(x)$

$$\frac{d^2 u}{dx^2} + (k^2 - \theta)u = 0$$

Substitution of Eq. shows that the new condition is fulfilled on the off chance that we characterize as

$$\theta(x) \equiv \frac{3k'^2}{4k^2} - \frac{k''}{2k} + (m^2 - 1/4) \frac{k^2}{\xi^2}$$

The development of k^2 in forces of x brings about the accompanying driving term in the extension of $\theta(x)$,

$$\theta(x) \xrightarrow{x \rightarrow 0} \frac{3(n+5)a^2}{2(n+4)(n+6)} - \frac{3b}{n+6}$$

Thus $\theta \ll k^2$ in the asymptotic district and isn't unimportant in contrast with k^2 in a region around turning point. But quite small value of indicates that for gradually shifting potential Eq. is a decent guess to genuine arrangement of Eq. For straightforwardness we consider the case comparing to direct defining moment $n=1$ as appeared in Fig. In district $^1 (x>0)$ Eq. is utilized while in district $^2 (x<0)$ Eq. is utilized.

Putting $\xi_1(x) \equiv \int_0^x k dx$ and $\xi_2(x) \equiv \int_x^0 \gamma dx$ with the goal that both ξ_1 and ξ_2 increments as moves from the defining moment, the two autonomous arrangements in every one of the two areas become

$$u_1^\pm(x) = A_\pm \sqrt{\frac{\xi_1}{k}} J_{\pm(1/3)}(\xi_1)$$

$$u_2^\pm(x) = B_\pm \sqrt{\frac{\xi_2}{\gamma}} I_{\pm(1/3)}(\xi_2)$$

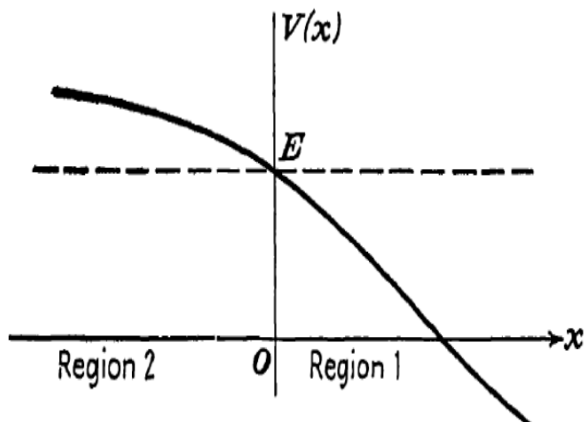


Fig. A typical linear turning point shall be indicated at the origin.

Increments as moves from the defining moment, the two free arrangements in every one of the two areas become

$$J_{\pm(1/3)}(\xi_1) \xrightarrow{x \rightarrow 0} \frac{\left(\frac{1}{2}\xi_1\right)^{\pm 1/3}}{\Gamma(1 \pm \frac{1}{3})}$$

$$I_{\pm(1/3)}(\xi_2) \xrightarrow{x \rightarrow 0} \frac{\left(\frac{1}{2}\xi_2\right)^{\pm 1/3}}{\Gamma(1 \pm \frac{1}{3})}$$

And $\xi_1 \equiv (2c/3)x^{3/2}$; $\xi_2 \equiv (2c/3)|x|^{3/2}$ the conduct of the u 's close is given as

$$u_1^+ \cong A_+ \frac{\left(\frac{2}{3}\right)^{1/2} \left(\frac{1}{3}c\right)^{1/3}}{\Gamma\left(\frac{4}{3}\right)} x,$$

$$u_1^- \cong A_- \frac{\left(\frac{2}{3}\right)^{1/3} \left(\frac{1}{3c}\right)^{-1/3}}{\Gamma\left(\frac{2}{3}\right)}$$

$$u_2^+ \cong B_+ \frac{\left(\frac{2}{3}\right)^{1/2} \left(\frac{1}{3}c\right)^{1/3}}{\Gamma\left(\frac{4}{3}\right)} |x|,$$

$$u_2^- \cong B_- \frac{\left(\frac{2}{3}\right)^{1/2} \left(\frac{1}{3c}\right)^{-1/3}}{\Gamma\left(\frac{2}{3}\right)}$$

Clearly u_1^+ joins smoothly on to u_2^+ if $B_+ = -A_+$ and u_1^- joins smoothly on to u_2^-

If $B_- = A_-$

These relations between the coefficients and the asymptotic developments

$$J_{\pm(1/3)}(\xi_1) \xrightarrow{x \rightarrow \infty} \sqrt{\frac{2}{\pi \xi_1}} \cos\left(\xi_1 \mp \frac{\pi}{6} - \frac{\pi}{4}\right)$$

$$I_{\pm(1/3)}(\xi_2) \xrightarrow{x \rightarrow \infty} \sqrt{\frac{2}{\pi \xi_2}} \left[e^{\xi_2} + e^{-\xi_2} \cdot e^{-\left(\frac{1 \pm 1}{2 \mp 3}\right)\pi i} \right]$$

Can be utilized to acquire asymptotic structures like Eq. for the two autonomous arrangements u^+ and u^- in two regions.

$$u^+ \xrightarrow{x \rightarrow +\infty} \sqrt{\frac{2}{\pi k}} \cos\left(\xi_1 - \frac{5\pi}{12}\right)$$

$$\xrightarrow{x \rightarrow -\infty} -\sqrt{\frac{1}{2\pi\gamma}} \left(e^{\xi_2} + e^{-\xi_2 - \frac{5\pi i}{6}} \right)$$

$$u^- \xrightarrow{x \rightarrow +\infty} \sqrt{\frac{2}{\pi k}} \cos\left(\xi_1 - \frac{\pi}{12}\right)$$

$$\xrightarrow{x \rightarrow -\infty} -\sqrt{\frac{1}{2\pi\gamma}} \left(e^{\xi_2} + e^{-\xi_2 - \frac{\pi i}{6}} \right)$$

The asymptotic type of any direct blend of u^+ and u^- can be found from these equations which might be utilized to acquire advantageous association recipes between the asymptotic WKB arrangements in the two districts. For example the mix $u^+ + u^-$ which contains just the diminishing exponential, yields the main association recipe

$$\frac{1}{2\gamma^{1/2}} e^{-\xi_2} \rightarrow \frac{1}{k^{1/2}} \cos\left(\xi_1 - \frac{\pi}{4}\right)$$

Eq. turns into the typical outspread condition if x is supplanted by r and $V(x)$ is supplanted by $V(r) + \frac{\hbar^2 l(l+1)}{2\mu r^2}$ which adequately speak to a potential barrier as appeared in Fig.

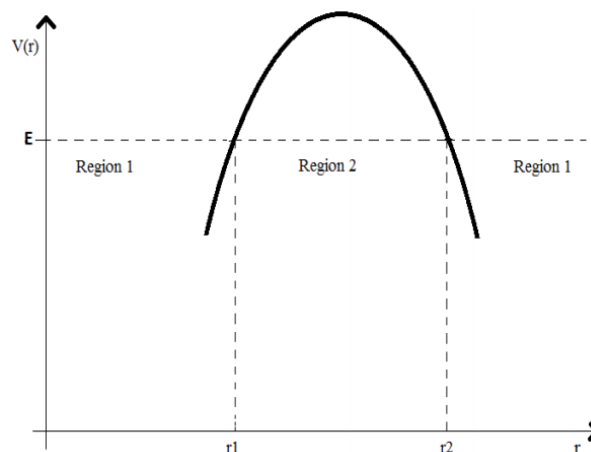


Fig. Single energy particle E, penetrating a barrier.

We have just observed that in area 2, the wave function is a genuine exponential of the structure.

On the off chance that the necessary $\int_{r1}^{r2} \gamma dr$ is obvious larger than solidarity then the conduct of the arrangement is ruled by large proportion of the wave function at the two defining moments. The proportion of the square of wave function is named as barrier entrance factor T and is given as

$$T = \exp\left[-2 \int_{r1}^{r2} \gamma(r) dr\right]$$

With

$$\gamma(r) = \frac{1}{\hbar} \left\{ 2\mu \left(V(r) + \frac{\hbar^2 l(l+1)}{2\mu r^2} - E \right) \right\}^{1/2}$$

RESULT AND DISCUSSION

Contributions of ICF in ${}^9\text{Be} + {}^{169}\text{Tm}$, ${}^{181}\text{Ta}$ and ${}^{187}\text{Re}$ Fusion Reactions

Right now present, alongside point by point conversation, the results of figurings of the fusion excitation functions for reactions actuated by 9Be on

${}^{169}\text{Tm}$, ${}^{181}\text{Ta}$ and ${}^{187}\text{Re}$ targets in close to barrier energy locale utilizing the code PLATYPUS wherein ICF and CF occasions are determined independently. Among different data sources, the centroid and width of the Gaussian function that approximates the spiral likelihood appropriation of projectile ground state wave function are significant fixings required in the figurings. So as to decide the spiral piece of the ground state wave function of the projectile it is accepted that the nucleus 9Be might

be approximated as a framework comprising of two loosely bound alpha particles. Due to the high likelihood of breakup of ^9Be into $^8\text{Be}^*$ and a neutron it is very legitimized to accept pseudo- ^8Be containing two alpha particles as projectile. The spiral ground state wave function of this alpha+alpha framework bound with 0.5MeV energy, under the presumption of a nodeless s-state, is gotten by understanding the concerned Schrödinger condition for Woods-Saxon potential with 32.66MeV, 1.25fm and 0.62fm as profundity, range and diffuseness parameters. The so gotten wave function is fitted with a Gaussian function with 2.17fm and 3.98fm as the centroid and width. Other than these, the parameters of the breakup function that is A_n and α are required in the figurings and are dictated by utilizing the trial breakup likelihood information at two unique estimations of $R_{\min}$ (or energy) in the region of Coulomb barrier. The estimations of the parameters A_n and α for various frameworks are recorded in table.

Table The estimations of breakup function parameters A_n and α alongside the breakup likelihood (PBU) at two distinct estimations of $R_{\min}$ used to decide A_n and α for various projectile-target

System	P _{BU}	R _{min} (fm)	A	α (fm ⁻¹)
$^9\text{Be}+^{169}\text{Tm}$	0.0108	15.1	2587	0.82
	Ref. [14]	0.0371		
$^9\text{Be}+^{181}\text{Ta}$	0.0185	14.5	4116	0.85
	Ref. [13]	0.0558		
$^9\text{Be}+^{187}\text{Re}$	0.00406	16.3	5644	0.864
	Ref. [14]	0.0315		

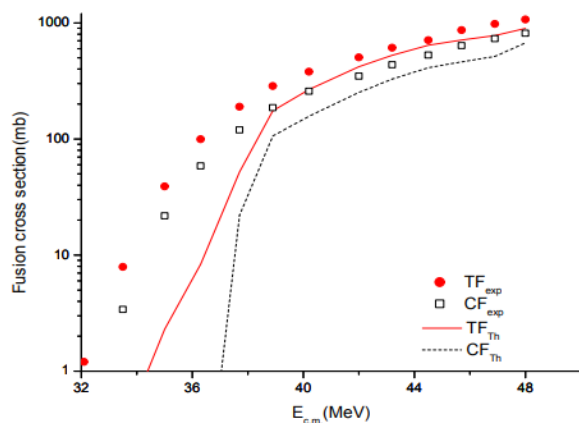


Fig. Fusion excitation functions for CF and TF systems, measured using PLATYPUS code, are contrasted with the corresponding data for $^9\text{Be}+^{169}\text{Tm}$ method taken from Ref.[14].

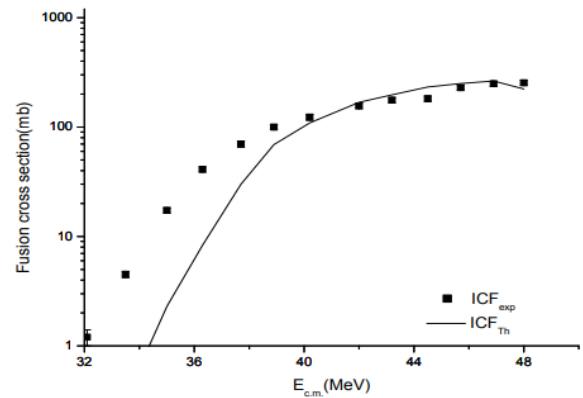


Fig. For the $^9\text{Be}+^{169}\text{Tm}$ device, the fusion excitation feature for the ICF cycle is contrasted with the corresponding data taken.

THE TUNNELING EFFECT

We have found in the former section that at energies higher than barrier energy the coordinating between the information and forecast is magnificent while at energies very near the barrier and a lot littler than the barrier the hypothesis totally neglects to clarify the information. The conspicuous explanation behind this conduct is that the quantum mechanical tunneling effects assume a noteworthy job in the close and sub barrier energy district. Attributable to nonappearance of tunneling in classical picture, no fusion is normal at energies littler than the barrier energy and subsequently the fusion cross section becomes zero quickly. Since the marvel of tunneling is a common quantum impact, it can't be presented in a model dependent on classical thoughts. Anyway an amendment factor emerging because of the quantum mechanical tunneling might be advantageously remembered for the investigation. Essentially, the quantum mechanical tunneling relates to non-zero likelihood of finding an item at a position where it is never watched classically. In the present case classically neither of the fragments is required to be inside the target. Be that as it may, quantum precisely there is a limited likelihood of finding it is possible that one or both the fragments inside the target prompting ICF and CF forms. Thus the absolute transition accessible for classically permitted NCBU channel decreases.

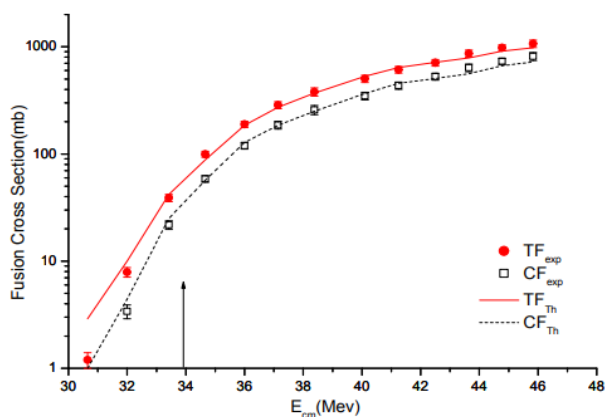


Fig. Fusion excitation functions for CF and TF processes, PLATYPUS code measurement with tunneling correction, was contrasted with the corresponding data for 9Be+169Tm method taken from Ref.[14].

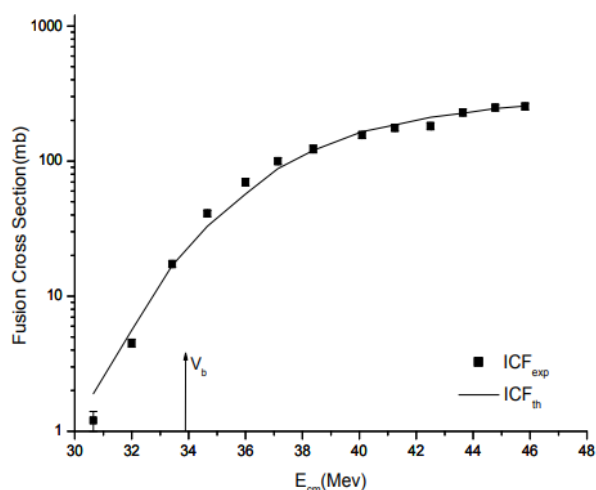


Fig. Fusion excitation function for the ICF process, calculated using PLATYPUS code with tunneling correction, is compared with the corresponding data for the 9Be+169Tm system taken from Ref.[14].

In Figs. the excitation functions of complete fusion and absolute fusion forms are contrasted and comparing information taken from Ref. [13] and [14] individually at around barrier energies for 9Be+181Ta and 9Be+187Re frameworks. The ICF excitation functions for these frameworks alongside the information taken from Ref. [13] and [14] are plotted in Fig. separately.

ENERGY DEPENDENT WOODS-SAXON POTENTIAL AND FUSION

Other than classical dynamical model, we have received an elective strategy to clarify the data which comprises in accepting that the commitment of ICF in TF is equivalent to that anticipated by code platypus for above barrier energy region and utilizing this presumption in a disentangled fusion model dependent on Wong's equation and energy subordinate Woods-

Saxon potential. Albeit any of the fusion model might be utilized for this reason, however this model is most straightforward one wherein different channel coupling effects are mimicked through the presentation of energy reliance in the potential. Utilizing this methodology we have examined the ICF, CF and TF excitation functions data for 9Be+181Ta and 187Re systems at around barrier energies. The so acquired fusion excitation functions for CF and TF reaction systems are contrasted and the relating trial data taken from Ref. [13] for 9Be+181Ta system are appeared in Fig. For above barrier energy region, fusion cross sections determined through code platypus and for underneath barrier energy region, counts are performed through EDWSP model.

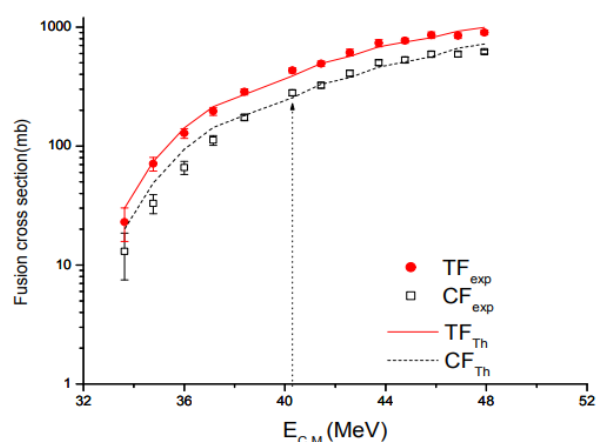


Fig. Fusion excitation functions for CF and TF 9Be+181Ta reaction, calculated using the PLATYPUS code at $E_{cm} > 1.14 V_B$ MeV and using Wong's EDWSP formula for $E_{cm} < 1.14 V_B$, are compared with experimental data from Ref.[13].

It is unmistakably observed that the CF data are very much clarified over whole energy system while the TF data are marginally under-anticipated in the profound sub-barrier energy region. Albeit the vast majority of the channels coupling effects are as of now imitated through energy reliance in potential, the slight confuse between TF data and forecast at profound sub-barrier energies might be credited to the way that the commitment of ICF is larger than that anticipated by code platypus. It might be seen all the more plainly in Fig. where ICF fusion excitation function is contrasted and the relating test data [13]. The coordinating among data and counts could be accomplished by considering 45–48% commitment of ICF in TF. Be that as it may, the so got information about the commitment of ICF in TF isn't unambiguous. By and by one gets a genuinely decent gauge in regards to the overall significance of ICF and CF systems in underneath barrier energy system. It is essential to make reference to here that the commitment of ICF in beneath barrier energy is more than that for above barrier energies.

For $9\text{Be} + {}^{187}\text{Re}$ system practically comparative results have been found as appeared in Figs.

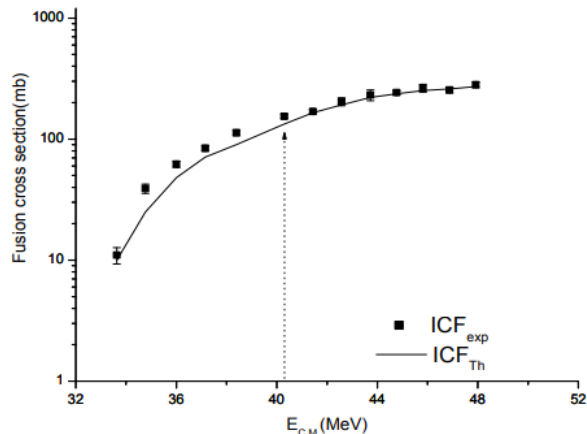


Fig. Fusion excitation feature for the $9\text{Be} + {}^{181}\text{Ta}$ reaction phase, determined using PLATYPUS code at $E_{\text{cm}} > 1.14$ VB MeV and using Wong's EDWSP method for $E_{\text{cm}} < 1.14$ VB, is contrasted with the experimental data taken from Ref.[13].

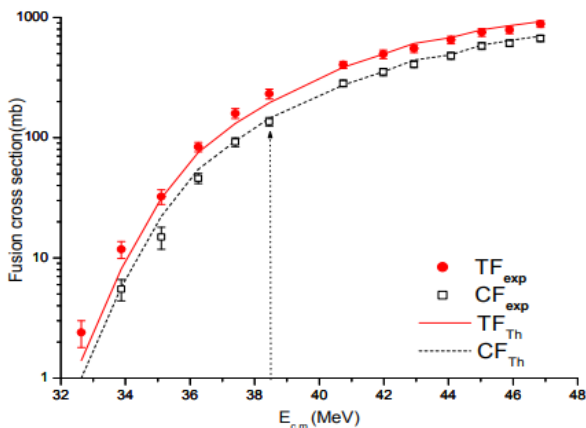


Fig. CF and TF cross section for $9\text{Be} + {}^{187}\text{Re}$ determined by code platypus (for $E / \text{VB} \approx 1.07$) and EDWSP model (for $E / \text{VB} \approx 0.07$) were compared to experimental data from Ref.[14].

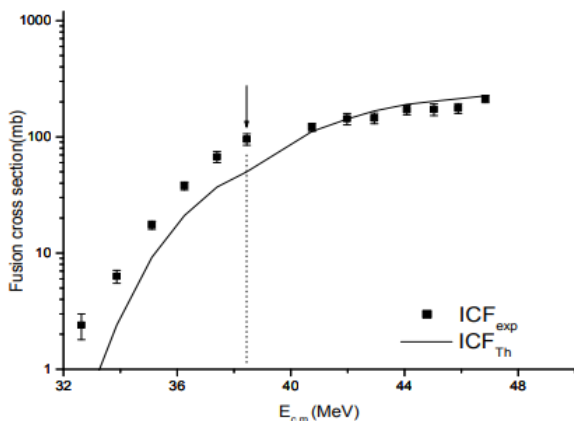


Fig. The $9\text{Be} + {}^{187}\text{Re}$ ICF cross section determined by code platypus (for $E / \text{VB} [1.07]$) and EDWSP pattern (for $E / \text{VB} [1.07]$) were contrasted with the experimental data from Ref.[14].

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Corresponding Author

Sarita Rani*

Research Scholar of OPJS University, Churu, Rajasthan