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**AN OVERVIEW IN SEISMIC WAVE
PROPAGATION IN DIFFERENT ANISOTROPIC
MEDIA**

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An Overview in Seismic Wave Propagation in Different Anisotropic Media

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Abstract – Seismology is the science that oversees seismic waves, examines the plans of the Earth and throws light into the actual science behind occasion of shakes. In this light, present assessment work provides for the theoretical examination of seismic wave multiplication in different anisotropic media with various material properties and computations repeating extended land conditions. A couple of customary seismic wave ponders like reflection/refraction, dissipating and moving weight issue have been inspected in seven issues contained in four free segments with layered Earth structure. A couple of mathematical strategies, for instance, Fourier change, Green's ability strategy, reformist assessment, division of variable, asymptotic turn of events, etc are used to decide the legitimate shut construction answer for expulsion of wave fields and summarized dissipating association for recently referenced wave ponders. The consistent eventual outcomes of each issue have been moreover dove into using particular assortment in appropriate limits and researched by graphical assessment (using MATLAB, MATHEMATICA and MAPLE programming). The hypothesis is composed in six critical areas, all of which gives a highlight on the theoretical pieces of seismic wave expansion. Seven issues are inspected in this proposition out of which four game plan with torsional and SH wave spread in different layered media close by various material credits. Different torsional modes are resolved and portrayed freely for effects of in homogeneity limits. Extent of suppression of torsional modes, joined effect of wave number and inhomogeneity extents and condition for non-dispersive torsional waves is resolved through numerical reenactment and portrayed using 2D and 3D graphs. Two issues focused in taking everything into account and refraction miracles of plane semi seismic waves in layered media between various monoclinic half spaces. The transitional layer between these half spaces is copied with isotropic/self-developed layer of restricted thickness in these two issues.

Keywords – Seismic Wave, Anisotropic Media

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INTRODUCTION

This paper presents a brief show of shake, seismology, seismic waves and flexibility. Since very antiquated past, the quake has been the central concern of individuals and a sweeping subject of sensible excursions. Shake is a speedy similarly as brief advancement of the Earth's surface, causing helpfully broken breaks of the Earth's surface. According to geologists, Earth has persevered through seismic quakes since countless years even before individuals showed up. Our ancestors acknowledged shudders as an incredible event "the criticism of Lord"; in any case in the term of Geology, seismic quake has been quite recently seen as a trademark event. The examination of quakes exists in the degree of a remarkable piece of Geophysics called Seismology. The term Seismology is the fundamental procedure for examination of quakes which relates seismic waves or sound waves with the geophysical activities in solid Earth. These seismic waves are created at a source, which can be both ordinary like quake, and phony, similar to impact, and induce through and around the

Earth. This request is totally navigated by a couple of advanced speculative seismology messages and incorporates an expansive assortment of applied math, actual science, inverse theory and observational data. The focal reason for theoretical seismology is to make and improve various systems for showing regional and overall scale geophysical cycles. Seismology includes a prodding position inside the new far reaching fields of Earth sciences and Geophysics. Seismology gives the degree of assessment to advancement instances of adaptable waves in various media. Varied interests and application consolidate finding the space of oil stores. A lot of the essential actual science isn't any more advanced than Newton's resulting law, $F = ma$ yet the difficulties introduced by conventional sources, structures and goliath data have moved present day mathematical meds and wide usage of unimaginable PCs. Seismology theory and examinations of Earth structure have a shock with the progress in instrumentation advancement and assessment. Setting up seismology, tracking down the major plan of the Earth was a long cycle and as a

piece of basic science to which various people from different countries contributed basically. The most key steps towards developing seismology and geophysics were taken at the completion of the nineteenth and the opening shot of the 20th many years. During this period, scientists contributed prominently to the headway of this new science and enormous quantities of their disclosures, revelations, and contemplations are still importance perceiving today. Nowadays seismology is for the most part drawn in with various applications like seismic source frameworks, Earth internal development showing, finding minerals, oil and combustible gas regions, arranging the multi-story structures, towers, ranges, acknowledgment of underground cavities under building districts, tremor safe constructions plans and columns, etc.

ELASTIC WAVES AS SEISMIC WAVES

Basic constituents of Earth are Silicates and Hematite. It has an extensive scope of sizes of force and warmth. The response of constituents is practically adaptable to little proportion of fluttering powers, in any case, viscously under the employments of trustworthy forces. This time dependence of the substance properties suggests that Earth "rings like a ringer", even as limited forces, for instance, surprising slip of rock across a deficiency surface or blast of a covered impact happened; while the fluid like movement of in general convection more than once reshapes the surface and inside the globe all through topographical time scales. The fireworks delivered by a tremor are eventual outcomes of adaptable waves (seismic waves) that are extended in spread. Material study of adaptable solids gives the degree of examination of seismic waves which is totally introduced by the theory of electrodynamics. Major sensible revelations about Earth's inside were made with the reflection/transmission illustration of adaptable wave inducing through Earth. Examination of seismic waves is the rule point of convergence of geophysical premium as inward constitution of the Earth can be found by inspecting these inciting flexible waves. The energy of these seismic waves going through the Earth's layers are eventual outcomes of a quake, spring of spouting magma or impact, gives out low repeat acoustic energy consistently recorded on seismographs. The repeat of seismic waves usually falls in the extent of generally 0.3 MHz to 100 Hz. These waves are important for:

- Mapping the minerals and solids inside the Earth.
- Finding prospecting oil and combustible gas regions.
- Determining the Earth structure.
- Blast showing, etc.

There are different kinds of seismic waves which move and partner in different habits inside Earth.

Exhaustively seismic waves are separated in two segments: (I) Body wave and (ii) Surface wave. The waves which spread through the Earth's inside are called Body waves, and are also assembled in two arrangements, specifically P wave and S wave. Nature of P wave is longitudinal in which particle development is facilitated in something comparable or converse course of wave multiplication and is similarly called fundamental wave. The second sort of body waves is S wave (discretionary wave) which is get over in nature. The S wave being a discretionary wave is enchanted in two inverse planes, the vertically hypnotized fragments, SV (or shear vertical) and the equally spellbound sections, SH (shear level). These two sections are vague by virtue of an isotropic medium; anyway are disengaged portions going at different speeds if the medium is anisotropic. Second piece of seismic waves is the surface waves, which are checked to outside surface of Earth layer by and large frame and the mantle. As we understand that, territory of Earth is round with restricted estimation, this leads us to dissect the outcome of the cutoff points on flexible waves spread.

These waves are named surface waves inferable from their limitation to the surface. Surface waves move slowly and have higher plentifulness appeared differently in relation to body waves. During shudders, surface waves have been exhibited more perilous due to their greater adequacy and moderate diminishing. These surface seismic waves are named Love wave and Rayleigh wave. A British seismologist A. E. H. Love [1] first expected the presence of Love waves in like manner called L-waves. The atom improvement during L-wave spread is restricted in the even plane just, while wave cause get over way. These waves are truly conveyed by SH waves guided in a surface layer at geographical condition, when S-wave speed is more unobtrusive than the secret medium. The presence of Rayleigh waves (or R-waves) was settled in 1885 by John William Strutt, Lord Rayleigh. The atom development in Rayleigh waves circles back to a vertical plane and follows bended way which is audit to the path stream of the wave. Retrograde elliptic development is a blend of get over and longitudinal wave. Overall, both Love and Rayleigh waves are dispersive in nature, in any case under some insignificant condition like homogeneous and level flexible development, Rayleigh wave gets non dispersive. Such a surface wave is moreover recognized as torsional surface wave, includes bending aggravations going through a medium like wire (Figure 1.1) or bar and is of dispersive nature with everything taken into account.



Figure 1.1: Tacoma Narrows Bridge (picture courtesy of Carleton University)

Torsional surface waves are constraint to upper crustal Earth and exist in only solid material as opposed to electromagnetic waves, which do propagate in gases, or liquid media. The study of torsional wave in elastic medium is very useful to seismologists because of its potential applications in non-destructive technology (NDT) and artificial explosions analysis.

WAVE PROPAGATION AND ELASTICITY

Wave multiplication is a very typical wonder of nature. It is remarkable that during tremor a monstrous proportion of energy is conveyed and brought out by seismic waves through and on the Earth surface. In all honesty Seismology is the science where we study the age, expansion, reflection/transmission, diffraction and other correspondence of these seismic waves on and inside the Earth. These seismic waves, when set off through normal/counterfeit sources, move completely outward from the foci and made transient nerves and therefore make lopsided characters in the stone, solids or other topographical media experienced. Likewise to consider the misshapening achieved by seismic waves, one need to suitably depict the adaptable properties of the spreading media close by its direct under external stacking using theory of adaptability, which finds its usage in valuable stone actual science, geophysics and planning issues. . Mathematical foundation of adaptability theory for understanding the fundamental seismological musings develops speculation of nervousness. Strain in a solid thing from a genuine perspective infers change perfectly healthy and estimation due to applied force (stress) which can be pliable, compressive or shear in nature. Contorting and stress in land media is regulated by adaptable constants of the material and power of the stacking. The brand name property of a body being adaptable addresses the restriction of accomplishing extraordinary equilibrium on removal of applied weight. From physicist see, stress is a second-demand tensor sum, portrayed as force per unit cross-section locale having unit as Newton per meter square $\square 2 \text{ Nm}$, all things considered implied by ij and circles back to the little surface with the conventional along i - th, and the force part planned towards the j - th direction. A pressing factor tensor $\square \square ij, 1,2,3 \square ij \square$ circling back

to a point in three-dimensional space is depicted by its 9 parts, and contains common and shear pressure components $\square \square 11 \ 12 \ 33 \ (, , , , ,)$

$$\sigma_{ij} = \begin{pmatrix} \sigma_{11} & \sigma_{12} & \sigma_{13} \\ \sigma_{21} & \sigma_{22} & \sigma_{23} \\ \sigma_{31} & \sigma_{32} & \sigma_{33} \end{pmatrix}.$$

On similar note strain, i.e. change in the relative position of adjacent points $) = , 1,2,3$ (e_{ij} is also a second order tensor quantity where i represent the direction of the axis perpendicular to the plain of strain and j denotes the direction of the strain. For homogeneous isotropic medium producing small strains (strain order $3 - 10 \leq$), general form of strain tensor $ij e$ is symmetric in

$$\text{nature and is defined as } e_{ij} = \frac{1}{2} \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) = e_{ji},$$

Where $) = (u \times i i i, 1,2,3$ respectively denote the particle displacement and unit vector in the i -th direction. In summary elasticity is a systematic investigation of stress, strain and displacement in an elastic body and it is a time independent material property, where stress -strain relation looks like figure 1.2 within linear elastic limit.

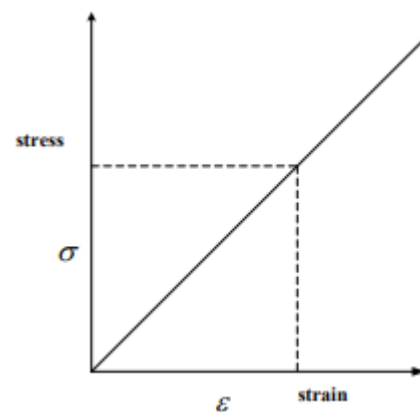


Figure 1.2: Stress- strain graph

Recently referenced model for direct adaptability fits well for transient rushed stacking anyway under long haul powers, stress-strain association depends upon time and this time-depending behavior of materials is explained using viscoelasticity theory. This term was established using two enunciations: thickness and adaptability; adaptability is a solid property while consistency generally shows security from stream in fluids. Thusly, geographical media showing viscoelastic lead is a mix of fluid and solid properties which follow the going with association.

$$\sigma = \eta \dot{\varepsilon}, \quad (1.1)$$

where σ is stress tensor, η is viscoelastic coefficient and $\dot{\varepsilon}$ is strain rate $\left(\frac{d\varepsilon}{dt}\right)$. Various researchers have proposed different viscoelastic models but for present research work, we have confined to Kelvin Voigt model. This model proposed by British physicist and engineer Lord Kelvin and German physicist Woldemar Voigt, can be represented schematically by a viscous damper dash pot () and purely elastic spring () connected in parallel as shown in the figure 1.3. The total stress σ applied to the whole system will be the sum of the stress in each component represented by following equation

$$\sigma = \sigma_s + \sigma_d, \quad (1.2)$$

where σ_s is the total stress of spring and σ_d is the total stress of dash pot.

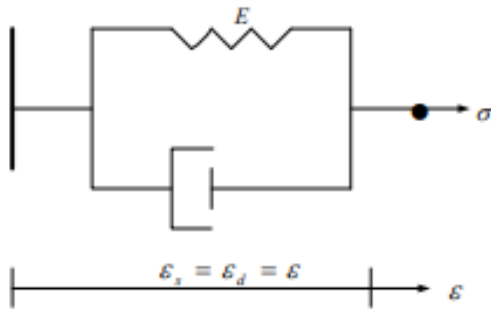


Figure 1.3: Schematic Kelvin Voigt model

Due to parallel arrangement of the two components, spring and dashpot will be deforming by an equivalent quantity, once the external stress is applied. Thus, the whole strain ε will be identically equivalent to the strains of spring () ε_s and dash pot () ε_d , represents by following equation

$$\varepsilon = \varepsilon_s = \varepsilon_d, \quad (1.3)$$

Applying Hooke's law for elastic (spring) and viscoelastic (dashpot) component:

$$\sigma_s = E\varepsilon_s, \quad (1.4)$$

$$\sigma_d = \eta \dot{\varepsilon}_d. \quad (1.5)$$

Substituting eq. (1.4) and (1.5) in eq. (1.2), we get

$$\sigma = E\varepsilon_s + \eta \dot{\varepsilon}_d, \quad (1.6)$$

from eq. (1.3), therefore

$$\sigma = E\varepsilon + \eta \dot{\varepsilon} = E\varepsilon + \eta \frac{d\varepsilon}{dt} \quad (1.7)$$

Equation (1.7) is called a linear first-order differential equation for Kelvin Voigt model.

PROPAGATION OF TORSIONAL WAVE IN A HOMOGENEOUS MAGNETO ISOTROPIC LAYER OVER AN INHOMOGENEOUS ISOTROPIC HALF SPACE

If we set $\mu_1 = 0$, i.e. absence of internal friction in the layer, then the imaginary part of generalized dispersion eq. (3.1.19) vanishes, while the real part (eq. (3.1.18)) of the generalized dispersion relation reduces to

$$\tan \left(\frac{2\nu_r \sqrt{1 - \frac{c^2}{c_1^2}} \sqrt{\pi\mu_1}}{\sqrt{(H^2 - 4\pi\mu_1)}} h \right) = \frac{2\mu_2^2 ab\pi}{\mu_1 \frac{2\nu_r \sqrt{1 - \frac{c^2}{c_1^2}} \sqrt{\pi\mu_1}}{\sqrt{(H^2 - 4\pi\mu_1)}} (4\pi\mu_2 a - H^2)^{\frac{3}{2}}},$$

where $c_1 = \sqrt{\frac{\mu_1}{\rho_1}}$, $c_2 = \sqrt{\frac{\mu_2}{\rho_2}}$, and ν_r is the real wave number.

PROPAGATION OF TORSIONAL WAVE IN A HOMOGENEOUS MAGNETO VISCOELASTIC LAYER OVER A HOMOGENEOUS SUBSTRATUM

When the frequency of in homogeneities in the lower half-space vanishes, (i.e. $0 \rightarrow b$), the generalized complex period eq. (3.1.17) reduces to

$$\tan(\xi_{17} - i\xi_{18})\nu_r h = \frac{-(\mu_2 a(-8\pi\eta a\mu_2 + \eta H^2))}{2\bar{\mu}_1 \beta_6 (\xi_{17} - i\xi_{18})\nu_r}.$$

Addresses the scattering connection for torsional wave proliferation in a magnetoviscoelastic isotropic layer over a homogeneous magneto isotropic base. Disentanglement of scattering connection in yields the scattering and ingestion relations of twist wave because of magneto-viscoelastic layer over a homogeneous isotropic magneto-versatile half space:

$$\frac{\xi_{21}(1 - \xi_{22}^2)}{(1 + \xi_{21}^2 \xi_{22}^2)} + \frac{(\mu_2 a(-8\pi\eta a\mu_2 + \eta H^2))(\xi_{17}\mu_1 + \omega\mu_1' \xi_{18})}{2\beta_6 \nu_r ((\xi_{17}\mu_1 + \omega\mu_1' \xi_{18}) + (\omega\mu_1' \xi_{17} - \xi_{18}\mu_1))} = 0,$$

$$\frac{\xi_{22}(1 + \xi_{21}^2)}{(1 + \xi_{21}^2 \xi_{22}^2)} + \frac{\mu_2 a(-8\pi\eta a\mu_2 + \eta H^2)(\omega\mu_1' \xi_{17} - \xi_{18}\mu_1)}{2\beta_6 \nu_r ((\xi_{17}\mu_1 + \omega\mu_1' \xi_{18}) + (\omega\mu_1' \xi_{17} - \xi_{18}\mu_1))} = 0.$$

CONCLUSIONS

The current investigation work adds to the speculative examination of seismic wave inciting in different anisotropic media with various material properties and computations mirroring grouped land conditions. Considering the Earth as a layered media, wave wonders like reflection/refraction, dispersing, and effect of moving weight have been discussed in seven

issues contained in four free segments. The logical eventual outcomes of each issue have been furthermore discussed using different assortments in significant limits and researched by graphical assessment using MATLAB, MATHEMATICA and MAPLE programming). The huge responsibility and finish of present work are summarized as follow: Two issues of tensional surface wave multiplication in different layered media have been discussed in paper. For tensional wave inducing, layered development model of Earth was proposed in Paper for generation with and without thickness sway. The chief issue of this Paper examinations the tensional wave expansion in inhomogeneous layer sandwiched between inhomogeneous half-spaces. In homogeneity in super and sub layer are similarly familiar with sensibly get the thickness and resoluteness assortment inside the Earth crustal region. Variable separation technique is used to find the summarized dissipating association. Three tensional modes are seen and analyzed graphically using MATLAB and MAPLE to see the assortment of stage speeds against dimensionless wave number for different potential gains of inhomogeneity limits. It is derived that the stage speed basically impacted by the wave number, yet moreover by different potential gains of in homogeneities limits.

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